ABSTRACT

A STUDY OF SEVERAL ODD-ODD s-d SHELL NUCLEI VIA THE (p,d) REACTION AT 35 MeV

By

James Allen Rice

States in ²²Na, ³⁴Cl, ³⁶Cl, and ³⁸K have been studied via the (p,d) reaction at an incident proton energy of 35 MeV. Reaction products were analyzed with the Michigan State University split-pole magnetic spectrograph. The deuteron spectra were recorded both with a single-wire, position-sensitive proportional counter, at a total resolution of ⁵⁰0 keV, FWHM, and on nuclear emulsion plates, with resolutions of 8-18 keV, FWHM. Levels to 6 MeV of excitation in ²²Na, ³⁴Cl, and ³⁸K, and to 8 MeV in ³⁶Cl have been observed and excitation energies assigned to an accuracy of ⁵¹1 keV per MeV.

Angular distributions were measured from 3° to 60° , with special emphasis on the region from 3° to 35° . This has allowed a precise definition of the forward angle shapes for $\ell=0$ and $\ell=2$ single neutron pick-up angular distributions in the s-d shell. A careful screening of deuteron optical-model parameters available from the literature was conducted in an effort to reproduce the experimentally observed

shapes via distorted wave Born approximation calculations. The best overall fits to pure ℓ -transfer distributions for the A>30 nuclei were obtained with standard finite-range, non-locality corrected calculations which include a density-dependent damping of the $V_{\rm pn}$ interaction. A good ℓ =0 fit to the $^{23}{\rm Na(p,d)}^{22}{\rm Na}$ data could not be obtained for calculations which also yielded good fits for the A>30 nuclei.

Spectroscopic factors, 1-values and parity assignments, and excitation energies from the present work are compared with previous experimental studies and recent shell model calculations. The agreement between the present experimental results and theoretical predictions is good for low-lying levels in the residual nuclei, but observed 1=3 angular distributions and spectroscopic factors for higher excited states indicate a need for consideration of 2 (or 4 or 6) particle excitations to the f-p shell in the ground state configurations of the A>30 target nuclei.

A STUDY OF SEVERAL ODD-ODD s-d SHELL NUCLEI VIA THE (p,d) REACTION AT 35 MeV

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For Linda, with whom all things are possible.

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I. INTRODUCTION

The nuclear shell-model assumes that a given number of nucleons occupy specified orbitals about an inert "core" much the same as atomic electrons move in orbitals in the electro-magnetic field of the nucleus. These "active" particles are assumed to be responsible for most observable properties of the nucleus. Indeed, spins, parities, and magnetic moments of many nuclei may be predicted solely on the basis of the number and kind of nucleons which occupy the last, or highest energy, subshell consistent with a systematic stacking of nucleons in the lowest unfilled orbitals.

A detailed theoretical description of the nucleus is assumed to be obtainable in terms of a Hamiltonian characterized by a sum of one and two-body matrix elements, which result from interactions of individual nucleons with the core and a two-body interaction between pairs of active nucleons, respectively.

Nuclei with mass numbers between 17 and 40 are members of the s-d shell, i.e., the last nucleons occupy the $\mathrm{ld}_{5/2}$, $\mathrm{ld}_{3/2}$ orbitals in the simplest picture. Shell-model calculations for these nuclei have shown considerable advancement in the last decade. Early works considered couplings only in the highest occupied orbit, with all other subshells comprising the core. Considerations of this sort led to predictions for only a small number of low-lying excited states. Calculations allowing two-orbital excitations

showed better agreement with available experimental data on spin, parity, and energy assignments for low-lying levels. Sophisticated computer codes and calculational techniques have allowed recent theoretical studies in which the basis states have been expanded to include the entire s-d shell. Both empirical and least-squares adjusted single particle energy parameterizations have been used for the one-body matrix elements, while theoretical and empirical two-body interactions have been studied. In general, the recent results show good correspondence with the data, particularly for those nuclei with either odd-even or even-even combinations of protons and neutrons. Calculated spectra for the oddodd nuclei, however, are often in even qualitative disagreement with experimental results. The structure of these nuclei appears to be most sensitive to the details of the nuclear Hamiltonian and, therefore, any descriptive theory for the s-d shell would be severely tested in its attempt to reproduce sound experimental data for the odd-odd systems.

A critical comparison of recent Hamiltonians most certainly relies on accurately observed properties of the odd-odd s-d shell nuclei. Excitation energies, spins and parities of nuclear energy levels and spectroscopic factors for single-nucleon transfer may be observed via direct reaction nuclear spectroscopy. Direct reactions take place in a time interval comparable to the time necessary for the projectile to traverse the target nucleus ($\sim 10^{-23}$ seconds)

and therefore, do not "see" collective effects in the target nucleus and are assumed to involve only one-step processes, i.e., the target nucleus is not excited above a ground state configuration before any particle transfer occurs. which the incident projectile absorbs a nucleon from the target nucleus (pick-up) or deposits a nucleon in the target nucleus (stripping) are called single nucleon transfer re-The target nucleus, therefore, undergoes a change in mass number (A) of $\frac{+}{-1}$ and the resulting residual nucleus may be left in any of its energetically and quantum mechanically allowed energy levels. In reality, any nuclear state may be described as a sum of weighted components, each corresponding to the probability that given shell model orbitals are populated by specified numbers of nucleons in particular angular momentum couplings. The spectroscopic factors observed in transfer reaction experiments are a measure of the overlap, a quantum mechanical correspondence, of initial and final state configurations. When only one nucleon is transferred, therefore, one expects to probe specific shell-model wave function components for the initial and final nuclear states.

The choice of an appropriate reaction for nuclear spectroscopy studies depends on the available projectiles, targets, and detection and analysis apparatus. The Michigan State University cyclotron provides high resolution proton beams with currents sufficient to allow experimental runs of

reasonable brevity. Several of the odd-odd s-d shell nuclei which can be reached through single-neutron pick-up from stable targets are 22 Na, 34 Cl, 36 Cl, and 38 K. Natural 23 Na and 39 K metals and isotopically enriched 23 Na- 35 Cl, 7 Li- 35 Cl, and 23 Na- 37 Cl compounds are commerically available. All are easily evaporated at moderate temperatures and thin targets may be routinely produced. The properties of the MSU cyclotron and split-pole magnetic spectrograph allow charged reaction product groups of closely similar energy to be clearly separated, detected and analyzed. The structures of 22 Na, 34 Cl, 36 Cl, and 38 K are, therefore, subject to study via the (p,d) reaction.

Precise excitation energies for these four nuclei have previously been assigned only to those states below the 3-4 MeV region. Any extension of the experimental understanding of these nuclei naturally includes a precise determination of higher lying energies. Accurate extraction peak centroids is allowed by the high particle group resolution (8-10 keV, FWHM) obtained on nuclear emulsion plates in the present work. A comprehensive spectrograph calibration scheme and least-squares fitting procedures have made possible the assignment of excitation energies in the residual nuclei to accuracies of \$1 keV/MeV of excitation. This represents a significant improvement over previous charged particle studies, allowing a more critical comparison with calculated spectra and the rationalization of the results

of different kinds of experiments. The spectrum analysis for these studies was performed with the computer code MONSTER2 (see APPENDIX A) on the MSU Sigma-7 computer.

In the direct reaction process, one may attempt to picture the nucleus as a sum of several sphericallysymmetric potentials. This approximation is the basis of the Distorted Wave Born Approximation (DWBA) predictions with which the present data are compared. Parities of energy levels in the residual nuclei, orbital angular momenta of the neutrons transferred in (p,d) reactions and spectroscopic factors may be assigned on the basis of such comparisons of individual experimental angular distributions with DWBA predicted distributions calculated for given neutron quantum numbers and appropriate final-state excitation energies. Shape comparisons yield the transferred neutron orbital angular moemtnum quantum numbers (1) and, hence, the parities of the residual states $(\pi_{residual}^{=\pi} target^{\pi} neutron)$ with $\pi_{\text{neutron}} = (-1)^{\ell}$). Magnitude comparisons indicate relative strengths for the 1-values involved in a given transition; hence, a measure of wave-function component amplitudes. Previous single neutron pick-up experiments ((p,d), (d,t), (3 He, α)) observed angular distributions which generally did not include angles smaller than 10°-15°. The present work measures distributions in to 30, providing a critical test of the forward angle DWBA shapes. of different currently popular proton optical model

parameters had little effect on the calculated (p,d) distributions. However, the DWBA-predicted differential cross-section shapes were found to be noticeably dependent on the choice of deuteron parameters. The experimentally observed shapes for pure $\ell=0$ and $\ell=2$ transfers in the A>30 nuclei were best reproduced when the interaction responsible for the reaction, $V_{\rm pn}$, was damped by a simulated nuclear matter density dependence, and a broadly based set of optical-model potentials was used to describe the outgoing deuteron. The empirical Q-dependence of the $^{23}{\rm Na}\,({\rm p,d})^{22}{\rm Na}$ shapes has not been successfully reproduced, particularly those for $\ell=0$ neutron transfers. All of the DWBA calculations were performed with the computer code DWUCK using standard Q-dependence techniques.

The results of the present experiments are presented in three autonomous sections, one for the combined 23 Na(p,d) 22 Na and 35 Cl(p,d) 34 Cl works, and one each for 37 Cl(p,d) 36 Cl and 39 K(p,d) 38 K. Each section includes a summary of pertinent previous experimental and theoretical studies, and the experimental and analytical techniques employed for the particular work under consideration. Theoretical implications of the present energy level, parity and single neutron pick-up spectroscopic factor assignments are discussed in conjunction with recently utilized shell-model Hamiltonians.

II. THE 23 Na(p,d) 22 Na AND 35 Cl(p,d) 34 Cl REACTIONS

II.1. Introductory Remarks

Recent shell-model analyses 1-4 of the nuclei in the regions A=18-24 and A=30-38 indicate that the nuclei whose structures depend most sensitively upon details of the model Hamiltonian are those which have odd numbers of both neutrons and protons. While the general features of the spectra of doubly-even and even-odd nuclei emerge more or less satisfactorily from such shell-model calculations, the calculated spectra of the doubly-odd nuclei are often even in qualitative disagreement with the observed level sequences. It thus appears that the definitive test of microscopic many-body theories of the spectroscopy of light-medium nuclei will come in the attempt to explain the rich store of details observed in the experimental study of these particular nuclei.

The nuclei ²²Na and ³⁴Cl are pivotal to understanding the structure of the s-d shell. In an s-d shell-model their wave functions are constructed of 6 particles and 6 holes, respectively. This number of active nucleons is large enough to allow the full consequences of the particularities of the two-particle component of the nuclear Hamiltonian to become manifest. At the same time, the dimensionalities of the model states are such that extensive theoretical work, in which the full s-d shell-model space is employed to describe the wave functions of these nuclei, is available. This

latter point is important because it allows the exclusion of the possibility that the theoretical results might be contaminated by effects arising from intra-shell basis truncation.

Shell-model calculations made with Hamiltonians of the Kuo-Brown⁵ type or with two-body matrix elements derived from simple central potentials fail to reproduce many simple aspects of the 22 Na and 34 Cl energy level spectra, such as, for example, the spins of the ground states. 1,2 Hamiltonians derived in less straightforward fashion have been used to achieve some improvement in the agreement between theory and experiment, but it seems fair to say that a full understanding of these systems has not yet been achieved. The aim of the present experiment, part of a systematic study of doubly-odd nuclei in the s-d shell, $^{6-8}$ is to provide definitive experimental information on some aspects of $^{22}\mathrm{Na}$ and $^{34}\mathrm{Cl}$ so that a more rigorous critique of present and future structure calculations is possible. The hope is that a clarification of the structure of the A=22 and A=34 systems will facilitate progress in understanding the behavior of the nuclei in the middle of the s-d shell, A=24-32, where the correct details of the effective two-body nuclear interaction are essential.

We present in this report the results of a study of the (p,d) reaction on ^{23}Na and ^{35}Cl at 35 MeV. The principle results obtained relate to excitation energies and angular distributions of states in ^{22}Na and ^{34}Cl , and the ℓ -values and associated spectroscopic factors of the neutrons picked up

in the formation of these levels. There is considerable experimental knowledge $^{9-14}$ of the levels of 22 Na and a rapidly growing body of data $^{15-23}$ on 34 Cl. Work relevant to the characteristics of the T=1 states of these nuclei has also been done with the nuclei 22 Ne 24,25 and 34 S. 26,27 Since an extensive particle-transfer study with good energy resolution is available 10 for 22 Na, a large amount of fundamentally new information was not expected to emerge from our 23 Na(p,d) 22 Na data. Rather, we aimed to obtain more precise experimental excitation energies for higher lying states, an alternate set of spectroscopic factors to complement those from the (3 He, 4 He) reaction, and, with the aid of the higher energy resolution of the present work, a clarification of a few (but important) questions concerning the low-lying states.

Our results for ³⁴Cl make a considerably more significant contribution to the state of knowledge about this nucleus. We are able to resolve many more states than has been possible in previous experiments²² and, even for easily resolved states, our extensive angular distributions provide evidence for reversing some previous \(\ell\)-value assignments. These \(\ell\)-values and their associated spectroscopic factors, and the precise excitation-energy assignment made in the 3-5 MeV region of excitation, serve to advance our experimental comprehension of the mass 34 system to a condition almost comparable with that of A=22.

The present data are of interest from a reaction theory standpoint also, in that the angular range, energy resolution, statistical accuracy, and large number of transitions combine to provide stringent criteria for evaluating the usefulness of ordinary DWBA calculations for the (p,d) reaction at these energies for medium-light nuclei. The value of this aspect of the present study is enhanced by the concurrent analyses of (p,d) data^{6,8} on neighboring nuclei.

II.2. Experimental Procedures and Results

The present experiments were performed with the MSU Cyclotron 28 and Enge-type 29 split-pole magnetic spectrograph. The beam energies for the various experimental periods ranged from 34.9 to 35.0 MeV, and beam currents on target ranged between 300 and 800 nanoamps. The beam on target had a coherent energy spread of about 20 keV, but by using dispersion matching 30 in the spectrograph in conjunction with the techniques discussed by Blosser, et al., 31 resolutions of better than 8 keV (FWHM) were obtained for 20-25 MeV deuterons at the focal plane under optimum conditions.

Particle detection at the focal plane was accomplished either with nuclear emulsions or with a position-sensitive wire proportional counter. 32 The latter type of data, limited to a resolution of about 50 keV by the characteristics of

the counter, was used to supplement and confirm the results obtained by scanning the nuclear emulsions.

Three different types of targets were used in the present experiment in order to circumvent the difficulty of obtaining a clean Cl target. Targets of LiCl (35 Cl enrichment $_{299\%}$) were used to obtain spectra free from sharp states which would arise from other chlorine compound contaminants. However, the continuous background resulting from the (p,d) reaction on the Li isotopes lowered the quality of these spectra and made it difficult to obtain accurate cross-sections for weak transitions. Sodium chloride targets (35 Cl enrichment $_{299\%}$) provided data on Cl transitions which nicely complement those from the LiCl targets. Finally, in order to remove ambiguities resulting from overlaps of peaks from Na and Cl levels, a target of Na metal was bombarded. All of these targets were fabricated by vacuum evaporation onto thin carbon foils.

Figure 1 displays spectra, measured at 14° with nuclear emulsions, which result from bombardment of the three types of targets used. These targets were of moderate thickness and the combined spectrograph-cyclotron energy resolution was not fully optimized, resulting in peak widths at half-maximum intensity of 15-20 keV. Representative particle groups in Fig. 1 are labeled as to energy of excitation. Figure 2 displays a spectrum measured at 8°, with a NaCl target, for

which the energy resolution for deuterons at the focal plane was at the best level obtained in this set of experiments.

The excitation energies measured for levels of 22Na and 34Cl in the present experiment are used to label the peaks in Fig. 2 and are presented in Tables 1 and 2. These energies are obtained primarily from spectra measured at 80, 11° , and 16° with a resolution of $_{\circ}8$ keV, FWHM. In the case of many weakly excited levels, these data were supplemented by the data from the thicker targets of all three compositions. The energies were assigned as follows. The nuclear emulsion plates were scanned with a computer-linked microscope system 33 in which a 25-cm-long precision screw served to position the plate under the microscope objective. A stepping motor on the screw served to increment both the plate position and a position signal which was read into the computer whenever a contact was activated to signal the observation of a track. In this way, the track-density spectra were generated with high accuracy and reliability as regards both peak positions and intensities. The dominant peaks in the spectra were then tentatively assigned to known levels in $^{22}\mathrm{Na}$, $^{34}\mathrm{Cl}$, $^{11}\mathrm{C}$, 15 O, 12 C, 35 Cl, and 23 Na for which accurate (≤ 1 keV uncertainty) excitation energies exist. All of these residual nuclei were formed from the (p,d) and (p,p) reactions on 35Cl, 23Na, and on the $^{12}\mathrm{C}$ and $^{16}\mathrm{O}$ contaminants in the targets. momenta of the deuteron and proton groups corresponding to

Figure 1. Complementary spectra from the (p,d) reaction on the ²³Na, ²³Na-³⁵Cl and Li-³⁵Cl targets, measured at 35 MeV and 140, as recorded on nuclear emulsion plates. The resolution of the deuteron groups is 15-20 keV, FWHM. Selected peaks are labeled with excitation energy assignments from the present work, the "boxed" values indicating levels in ³⁴Cl.

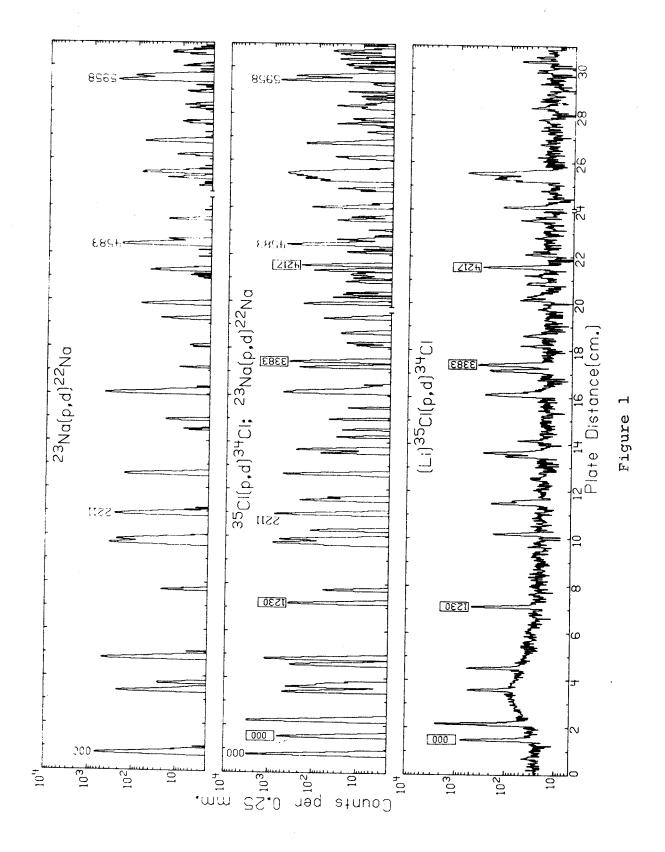
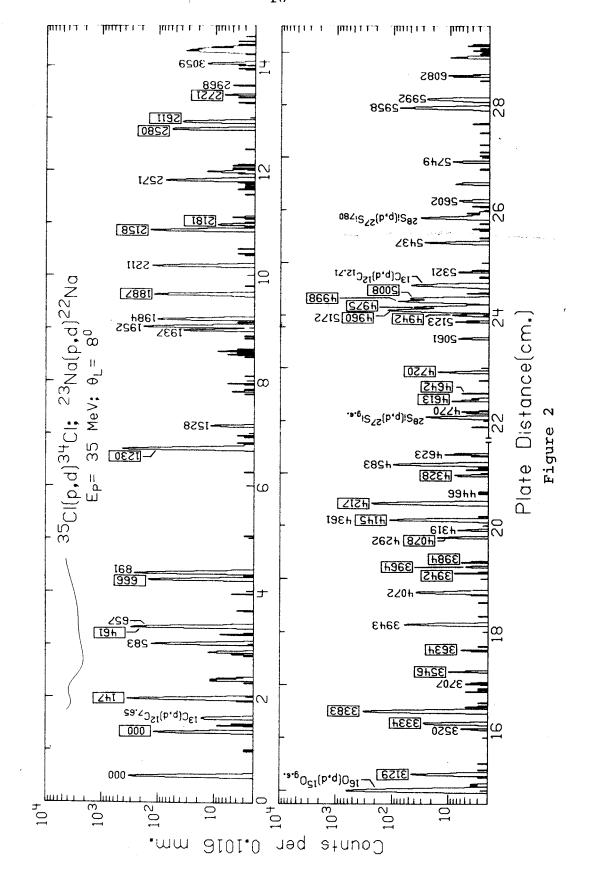


Figure 2. A spectrum from the (p,d) reaction on the

²³Na-³⁵Cl target, measured at 35 MeV and 8°, as
recorded on nuclear emulsion plates. The resolution of the deuteron groups is 8 keV, FWHM.
All excitation energy values are from the present
work, with those "boxed" indicating levels in ³⁴Cl.



population of these states were then calculated from the nominal settings and operating parameters of the cyclotron (beam energy) and spectrograph (scattering angle, magnetic field strength, position of emulsion plates, and non-linear corrections to the focal plane position vs. radius of curvature line) and from the nominal Q-values for the reactions. When the total spectrum spanned two emulsion plates the gap between the plates was also specified.

At this point all, or any desired subset, of the above parameters were adjusted so as to produce a least-squares fit between the set of precision energies used as input and the energies calculated to correspond to the measured peak posi-The changes in the nominal parameter values which occur when an adequately large data set is used as input are well within the experimental uncertainties associated with the various parameters. For example, typical beam energy changes are ≤ 10 keV out of 35 MeV, angle changes are $\leq 0.1^{\circ}$, and plate-gap changes are 0.0 to 0.1 mm. The appropriate final calculated excitation energies agree with the input values to $\stackrel{+}{-}1$ keV on the average. As input, we used essentially all level energies in ²²Na and ³⁴Cl below 3 MeV excitation, 15,18,34 the ground 34 and first excited states 67,89 of 11C and 12C, the ground states 34 of $^{15}\mathrm{O}$ and $^{16}\mathrm{O}$, and the ground 34 and first two excited states 68,97 of 23 Na and 35Cl.

We found that a statistically significant better fit to the input energies could be obtained if the \$^{35}Cl(p,d)\$^{34}Cl Q-value was changed from its nominal value\$^{34}\$ of -10.422 MeV to -10.420 MeV and the \$^{23}Na(p,d)\$^{22}Na Q-value was changed from -10.193 MeV to -10.195 MeV. These changes are not inconsistent with the assigned uncertainties of the nominal Q-values,\$^{34}\$ and at any rate, the excitation energy assignments depend only slightly upon whether the nominal or the adjusted Q-values are used. The levels whose excitation energies are of primary interest fall in the middle 15 cm of the 50 cm (two adjacent 25 cm plates) of exposed emulsion. The 15 cm on either side of this region are thus simultaneously calibrated to many precisely known energies and this calibration is interpolated into the middle region, where it is confirmed by one or two additional known states.

The uncertainties we assign to the excitation energies listed in Tables 1 and 2 are consistent with the scatter obtained both in analyzing the same data with different variants of the analysis procedure described above and in analyzing data taken at different angles with the same procedural details. The uncertainties are compounded from jitter in the measured peak positions, irregularities in the detailed magnetic field and focal plane structure, and inaccuracies and incompleteness in the set of input energies.

The angular distributions we present for the $^{23}\text{Na}(\text{p,d})^{22}\text{Na}$ and $^{35}\text{Cl}(\text{p,d})^{34}\text{Cl}$ reactions were compounded from all of the

Table 1. Excitation energies, ℓ = values, J^{π} and T values, and pick-up spectroscopic factors for states of 22Na. All C²S values extracted from the present data have been normalized to yield 0.59 for the ground state.

Ex (keV)		εeV) J ^π ,Τ		la+ ²² Na)	100 x $C^2S(l), C^2S(l+2)=-(23Na+22Na)$				
000ª	000 ^{b,c,d}	3 ⁺ ,0 ^b ,c,f 1 ⁺ ,0 0 ⁺ ,1	2ª	2° 2 2	,59ª	,59 g	,59 ^C		
583±1	583	1+.0	ດ້າ	2	2,19	1,22	,39		
657±1	657	0+11	0,2	5	,2	, 1	,24		
891±1	891	. 4+ U	2	2	,47	,58	,<7		
528±1	1528	5 ⁺ ,0 1 ⁺ ,0	-	-	37 /	,,,,,	•57		
937±1	1937	1 † n	0		3,	a a.			
952±1	1952	2+,1 3+,0	2	2	μ1	$\frac{3}{7}, \frac{3}{49}$,57		
984±1	1983	3+30	2	2	,41 ,26	,37	,29		
211±1	2211	1-,0	ī	2 1	77	, 37	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		
571±1	2572	2-10	ī	î	20,		27, 21,		
968±2	2969	2-,0 3',0 2',0	(2)	(2)		,13	***		
059±1	3059	2+,0	`2	2	, 3	0, 3	,<2 , 3		
520±1	3521	3-10	(3)	•	,(2)	0, 3	, ,		
707±2	3708	3-,0 6+,0	()		, (2)				
943±2	3944	1+,0	0,2	0	1, 3	2, 0	3,		
072±2	4069	ų+ <u>,1</u>	2	2	,12	14,14	,17		
292±3	4294	.0	-	•	71.6	17,17	,		
319±3	4319	1+,0	0,2		<1 1	1 0			
361±2	4360	2+,0 (4-),0 (7+),0	0,2	0,2	<1, 1 1, 5	1, 0 4, 3	2, 2		
466±3	4466	(4-).0	٠,٠	٠,٠	1, 3	7, 3	2, 2		
525±4	4522	(7+).0							
583±2	4583	2-,0	1	1	40,		24		
623±2	4622	- 0	-	•	40,		34,		
	4708	(5 ⁺) 0							
770±2	4770	0-4+ 0		(2)					
061±4	5061	1-2+,		0,2			, 9 1, 2		
096±4	5099	,		٠,٠			1, 2		
123±3	5117								
172±3	5165	(2)+,1	0,2	0,2	2,18	, 9	7 15		
321±3	5317	· ,-	~,-	٠,٠	-,	, ,	, 410		
437±3	5440	- ,	1	1	11,		8,		
602±3	5605	,	•	0,2	,		1, 2		
719±4,		, , ,		٠,٠			-, -		
749±4 ³	5740								
826±6	5830			n.s.					
861±5	5858			0,2			<1, 2		
	5938			- , -					
958±4	5953	,1	1	1	50,		58 , ,13		
992±4	5995	,-	2	2	,15		13		
082±4	6088		•	•	,		94 J		

^aPresent work. ^bReference 9.

eReference 13.

fReference 12.

CReference 10.

gReference 4.

dReference 11.

Excitation energies, ℓ_- values, J^π and T values, and pick-up spectroscopic factors for states of ³⁴Cl. All C²S values extracted from the present data are normalized such that C²S=0.35 for the ground state. Table 2.

	Ex (keV)		J^{π} ,T		L	100	x C ² S(£	.),c ² s(2+2)(³⁵ C1+ ³⁴ C1
000ª	000 ^b ,c	,d e	0 ⁺ ,1 ^b ,c,d 3 ⁺ ,0 1 ⁺ ,0	2 a	2 d	25	,43	f		, h
147±1	146		3+ 1n	2	2	, 35	,43	•	318	, 45 h
461±1	461		1+,0	0,2	0,(2)	,105		,	TOP	, 120
66611	666		i+,0	0,2		11, 23		18,	15	0, 28
230±1	1230		2+,0	0,2	2,(0)	4, 28		1,	32	16, 0
887±1	1888		2+,0	0,2	(0)	23, 20		18,	9	50, 0
158±1	2159	2127	A * * *		2	5, 11		2,	14	16, 0
181±1	2181	,	2 2 1 0	0,2	2	8, 11	12,	5,	11	32, 0
377±3	2377		2,4+,0	(2)		, 4		,	0	assume J=2
580±1	2579		4 ⁺ ,0 1 ⁺ ,0	0,2	(0)	, 3			0	
611±1	2611		· ,0	2		5, 5		0,	4	
721±2	2722		2-,0	3	(2)	, 25		ο,	42	assume J=4
129±2	3126		2-,0 1+,0	0,2	3 2	, 3				
334±2	3332		1,0	2	(2)	1, 20		4,	6	
383±2	3381	3303	2 ⁺ ,1 3 ⁻ ,0 4(-),0			, 25		,	34	assume J=3
546±2	3545	0000	3- 0	0,2	2 1	26, 25	35,	25,	12	75, 0
602±3	3601		4(-),0		1					
634±3	3632		5-,0							
	3771		1-,0		3					
865±5			1,0		(1)					
942±4	394(0)	3914	0+,1							
964±4	03.(0)	3314	· , -					,	1	
984±4	3982		3-,0		•					
078±4	4075		μ - 0		3 3					
145±4	4140		4-,0 2-,0 1 ⁺ ,1							
		4072	1+ 1		1,3					
217±2		{ 40/2 4115	2+,1	0 2		36		, 17,	4	
328±4			2 ,1	0,2		16,20	30,	{ °°,	18	30,0
	4352		(1)-,0		-					
	4416	/1	-3)-,0		1					
+65±5	4460	(2	-37,0		Ţ					
	4514	(2	,3)-,0 (2)-,0		1					
513±4	4605	/1	(2),0							
342±5	4636	HE33/3	-3)-,0		1					
720±5	4720	4622(1 4687	-3)-,1	_	1					
360±6	7/20	400/		2		, 21	,21		5	
942±5		(4875)	(3+)			-	-	,		
142±5		(4891)	(2+)							
	407603		.+ .							
75±5	497(0)	5227	0,1				,40			
98±3							•			0,170
08±3		5318								V 9 A 1 U
60±6		5380								

^aPresent Work.

bReference 15.

CReference 16.

eEnergies for states in ³⁴S; References 26,27.

fSpectroscopic factors for ³⁵Cl(d, ³He) ³⁴S; Reference 25.

gReference 2.

hReference 22.

data accumulated from the different targets and with the different detection mechanisms. Of course, when lack of resolution prevented unambiguous values from being obtained in particular cases, such data were rejected. Also, in some cases the track density of strongly excited levels was too high to permit accurate counting by the scanners, so that counter data alone was relied upon. The angular distributions for states in ²²Na are shown in Figs. 3, 4, and 5 and those for levels in ³⁴Cl in Figs. 6 and 7. Not all states listed in Tables 1 and 2 could be observed at enough angles to permit measurement of meaningful angular distributions. These states were at best weakly populated and are not included in Figs. 3-7.

The cross-section scales in Figs. 3-7 were assigned by comparing the (p,d) differential cross-sections as measured with the wire proportional counter to the (p,p) elastic differential scattering cross-sections in the vincity of the maximum in the 30°-50° region. The counting rates for the elastic scattering were manageable for the counter in this region and the Na and C1 peaks could be resolved clearly. The elastic scattering distributions were normalized to the predictions obtained from the Becchetti-Greenlees optical model potential formula 37 (see APPENDIX B). The experimental angular distributions for 23Na and 35Cl in this region are rather dissimilar and both were simultaneously well fit with the Becchetti-Greenlees predictions. We estimate a 10% uncertainty for the

accuracy of the optical model cross-sections in this region, and estimate a 10% probable error for the mechanics of relating the experimental (p,d) yields to the (p,p) yields. Thus, the combined total uncertainty in the overall cross-section normalization of our angular distributions is estimated to be in the range of 15%.

The relative uncertainties from distribution to distribution should be less than 2%. The chemical stability of sodium chloride appears to be maintained under evaporation and bombardment, so the relative Na to Cl cross-sections should also be good to 2%.

II.3. Analysis of the Angular Distributions

The angular distributions displayed in Figs. 3-7 were analyzed with the distorted-wave Born approximation (DWBA) 38 to obtain ℓ -values for the neutrons transferred in the (p,d) pick-up process and the associated strengths, or spectroscopic factors. This analysis was carried out by least-squares fitting a combination of $\ell=0$ and $\ell=2$ (or $\ell=1$ and $\ell=3$) curves, predicted for a transition of given Q-value, to the $3^{\circ}-35^{\circ}$ experimental data for each state. The solid curves in Figs. 3-7 show the combined- ℓ theoretical distribution fits from which the spectroscopic factors were obtained. The dotted curves indicate the contribution of the smaller ℓ -value pattern to the combined (solid line) distribution curves.

Figure 3. Experimental angular distributions for states in \$^2Na\$ as observed in the \$^3Na(p,d)^2Na\$ reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated \$\ell-\value\$ for mixed-\$\ell\$ distributions.

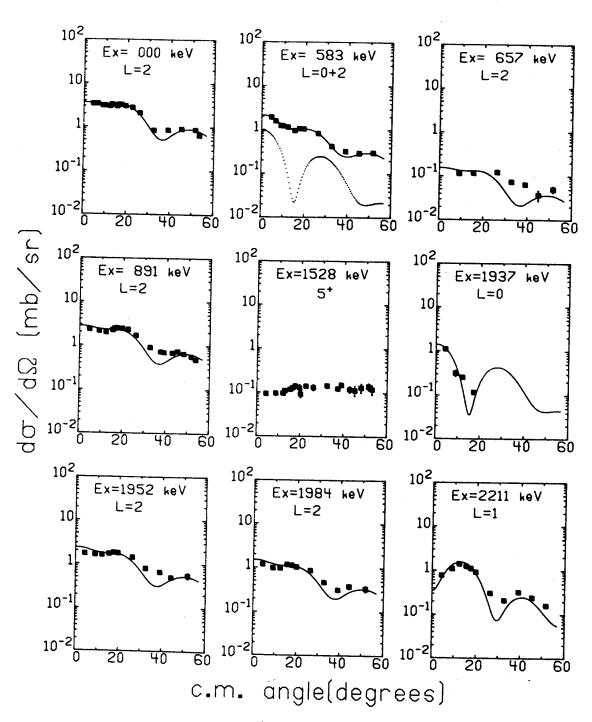


Figure 3

Figure 4. Experimental angular distributions for states in ² Na as observed in the ² Na (p,d) ² Na reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated \(\ell-\text{value}\) for mixed-\(\ell\) distributions.

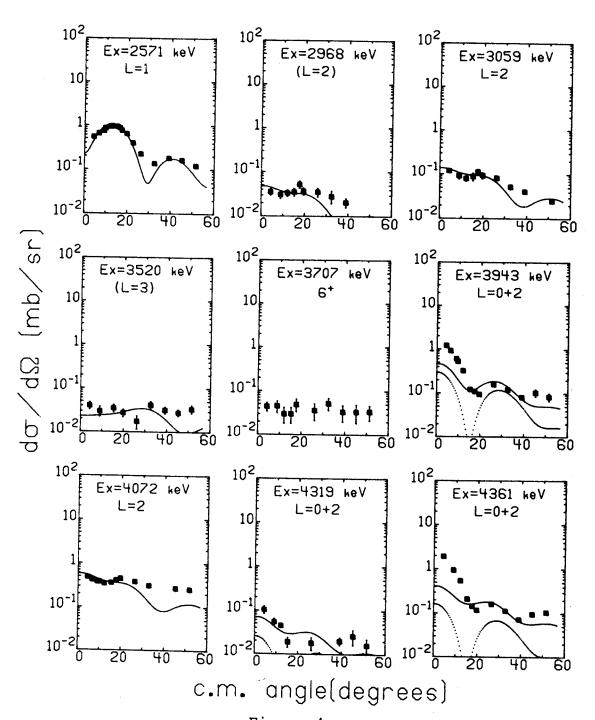


Figure 4

Figure 5. Experimental angular distributions for states in ²²Na as observed in the ²³Na(p,d)²²Na reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated l-value for mixed-l distributions.

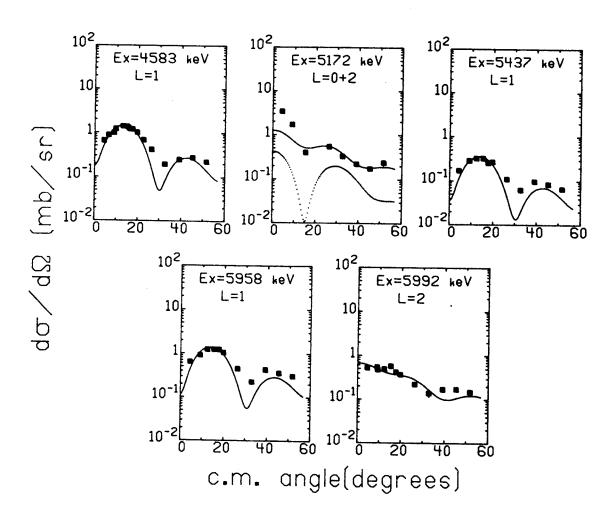


Figure 5

Figure 6. Experimental angular distributions for states in ³ ⁴Cl, as observed in the ³ ⁵Cl(p,d) ³ ⁴Cl reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated l-value for mixed-l distributions.

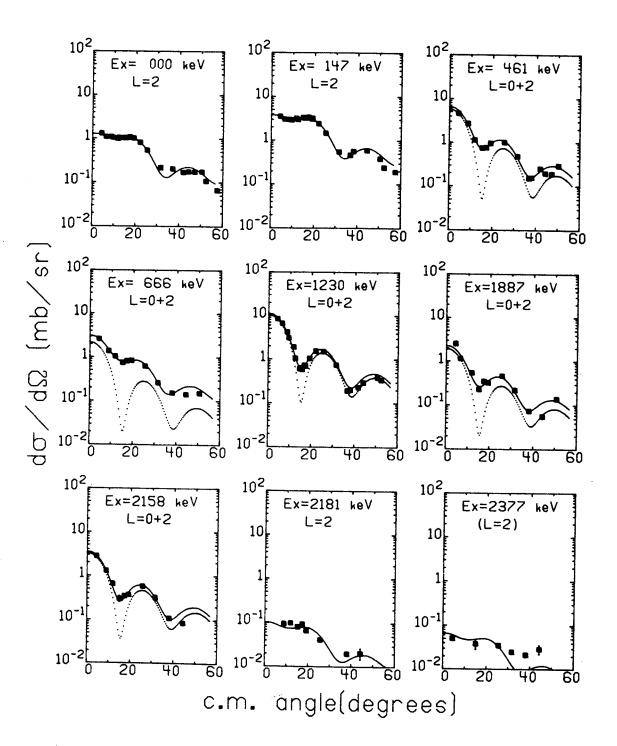


Figure 6

Figure 7. Experimental angular distributions for states in ³ Cl, as observed in the ³ Cl(p,d) ³ Cl reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated \(\ell-\)-value for mixed-\(\ell\) distributions.

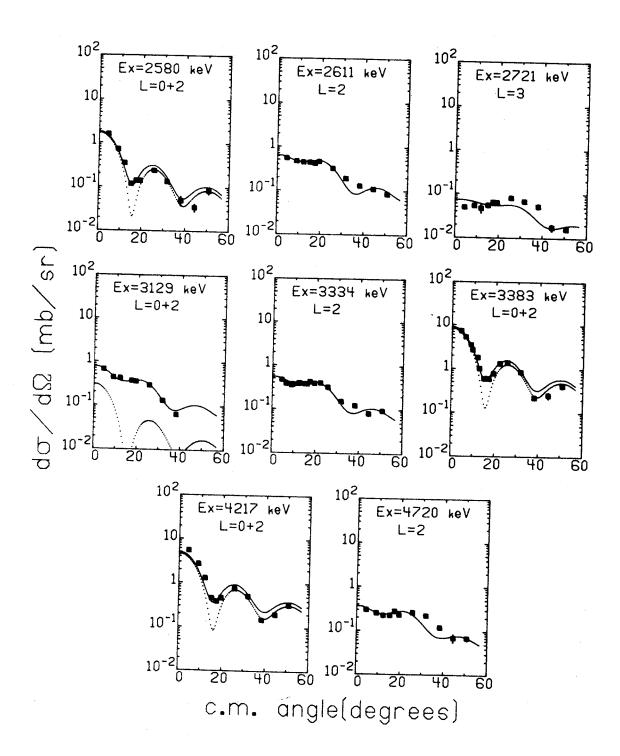


Figure 7

Many previous studies of the (p,d) and (d,p) reactions in the 15-40 MeV range of particle energies have experienced serious difficulties in analyzing the experimental angular distributions with the DWBA. Detailed studies ^{39,40} on ²⁰⁸Pb and ¹⁶O are particular examples. The difficulties involved obtaining good fits to given \(\ell\)-value transitions at particular energies and maintaining stable, good fits and consistent spectroscopic factors over a range of \(\ell\)-values, beam energies, and Q-values. Problems specifically involving the relationship between DWBA predictions and experiment as a function of the Q-value of the reaction (corresponding to different bindings of the transferred neutron to the core) have been studied extensively ^{41,42} in the f-p shell with the aid of sum-rule arguments.

A general feature of past DWBA analyses of (p,d) angular distributions has been that the local, zero-range predictions were improved, vis a vis the experimental shapes, by introducing a cut-off in the radial integration somewhere near the nuclear surface. It has been proposed and demonstrated 44-47 that an alternate prescription, the "adiabatic" deuteron, to the usual elastic-scattering-based deuteron optical model potential can, in a more physically motivated way, provide all of the benefits obtained by the use of cut-offs. A second alternative, also more plausible and successful than the sharp cut-off technique, involves making finite-range and

non-locality approximation corrections and, in addition, introducing a density-dependent damping of the $v_{\rm pn}$ interaction. 48

The many angular distributions obtained in the present experiment, measured with good statistical accuracy and energy resolution in the 4°-40° angular range, provide the basis for a very thorough critique of current DWBA procedures for (p,d) reactions on medium-light nuclei. We have carried out DWBA calculations using a variety of different prescriptions for the various input parameters and have compared the results with our data.

The present DWBA calculations were all made with the computer code DWUCK. The parameters of the optical model potential for 35 MeV protons were obtained from the formulae of Becchetti and Greenlees. The formulae of Fricke, et al., optical discernably different elastic scattering angular distributions for s-d shell nuclei, but the DWBA predictions for (p,d) seem largely insensitive to changing from one proton potential to the other.

When any of the conventional 51-55,98 deuteron optical—model potentials are used, the calculated shapes of the \$\ell=0\$ and \$\ell=2\$ distributions agree much better with our experimental test cases in the finite-range, non-local (FRNL) approximation than in the local, zero-range (LZR) approximation. (The non-locality parameters used were the standard values of 0.85 and 0.54 for the proton and deuteron, respectively.) The best

results obtained with any of these various potentials appear to be obtained with the "Set I" values of Hinterberger, et al. 51 (see Table 3), which is gratifying since this potential is probably the best grounded in terms of mass and energy dependence. The Hinterberger et al. "Set II" and the Newman, et al. 52 potentials yielded results very similar to each other and not too different from those of "Set I".

The critical success of Hinterberger "Set I", relative to potentials of different origins, lies in its correct reproduction of the forward angle $(\Theta_{Cm} \leq 20^{\circ})$ l=0 and l=2 shapes. Its principle failing, shared by all the others to a greater or lesser extent, is its overestimation of cross-sections at larger angles $(\theta_{cm} \ge 30^{\circ})$, a failing which grows more pronounced as the Q-values become more negative (excitation energies increase). Previous investigations led us to expect that both the "adiabatic" 43 and the "density-dependent" 46 alterations to the conventional DWBA procedure would improve the predictions at these larger angles. The "adiabatic" potential, designed to account for effects resulting from disassociation of the deuteron, is put together from proton and neutron optical model potentials (taken from Ref. 37 in the present instance) according to a particular prescription. 43,44 The adiabatic-potential calculations were carried out in the LZR approximation, since the FRNL corrections did not yield significantly different results.

Optical-model parameters used in the analysis of the $^{23}{\rm Na(p,d)}^{22}{\rm Na}$ and $^{35}{\rm Cl(p,d)}^{34}{\rm Cl}$ data. Table 3.

Particle	V _R (MeV)	r _R a _R (fm) (fm)	a _R (fm)	W _V r _V a _V (MeV) (fm) (fm)	r _V (fm)	a _V (fm)	WSF (MeV)	rSF (fm)	a _{SF} (fm)	V _{SO} (MeV)	rso (fm)	aso (fm)	r _c (fm)
23 Na(p,d) 22 Na:													
Protona	45,39	1.17	1.17 0.75	5.0	1.32 0.54	0.54	3.57	1.32	1.5.0	6.2	1.01	0.75	1.17
Deuteron (FRNL and	84.89-0.35 Ecm	1.25	0.743				13.0	1.25	0.723	6.0	1.25	0.743	1.30
Deuteron ^c (ADIABATIC)	102,59 ^d	1.17	0.779	1.17	1.29	0.589	1.17 ^d 1.29 0.589 17.33 ^d	1.29	0.583	6.2	1.01	1.01 0.75	1.17
35C1(p,d)34C1:													
Proton ^a	45.57	1.17	0.75	5.0	1.32 0.53	0.53	3,39	1.32	1.32 0.53	6.2	1.01	1.01 0.75	1.17
Deuteron ^D (FRNL and	86.92-0.35 Ecm	1.25	0.733				13.0	1.25	1.25 0.755	0.9	1.25	0.733	1.30
Deuteron ^C (ADIABATIC)	103.41 ^d	1.17	1.17 0.779	1.13	1.29	0.589	1.13 ^d 1.29 0.589 17.41 ^d	1.29	0.583	6.2	1.01	1.01 0.75	λ.,
Neutron Bound State	Adjusted to match separation 1.24 0.65 energy	1.24	0.65							λ=25			1.24
Reference 37.						dval Q-d	dvalues shown are for E = 0.00 MeV only; Q-dependence is as given in Reference eron hath meactions	mare te is a	for Exis	0.00 Me in Re1	eV only Ference	37.	

Reference 37.

^bReference 51.

^cReference 43; proton and neutron parameters from Reference 37.

For both reactions.

The "density-dependent damping" of the $V_{\rm pn}$ interaction 48 provides an alternate means to reduce cross-sections at larger angles. We use here the damping factor $F(r)=(1.0-1.845\rho\ (r)^{2/3})$, where $\rho\ (r)=0.17[1+\exp(x)]^{-1}$, $x=(r-r_{\rm o}A^{1/3})/a$ and " $r_{\rm o}$ " and "a" are the radius and diffusivity of the neutron bound-state well. The density-dependent $V_{\rm pn}$ damping was studied in conjunction with FRNL calculations which used the Hinterberger, et al. "Set I" deuteron potentials.

We have analyzed our data in detail with the following DWBA calculations (see Table 3): (1) The Becchetti-Greenlees 37 proton parameters and Hinterberger, et al. 51 "Set I" deuteron parameters, using the FRNL approximation. These calculations, henceforth referred to as FRNL, are thus completely orthodox and unadjusted. (2) This same combination of proton and deuteron parameters and computational approximations, but with the addition of the density-dependent damping of the Vpn interaction, henceforth referred to as DFRNL, and (3) The Becchetti-Greenlees proton parameters and the adiabatic deuteron parameters in the LZR approximation, henceforth referred to as ADIABATIC.

The results of these three types of DWBA calculations are compared with each other and with some of our experimental data for the 35 Cl(p,d) 34 Cl reaction in Fig. 8. The virtue of the DFRNL shapes is clearly evident over the range of excitation energy in 34 Cl shown therein.

Figure 8. A comparison of fits to representative angular distributions from the ³⁵Cl(p,d) ³⁴Cl reaction at 35 MeV with the three chosen types of DWBA calculations. All fits were performed over the angular range from 30 to 35°. The curves are identified as follows: ——DFRNL, ————FRNL, and ———ADIABATIC.

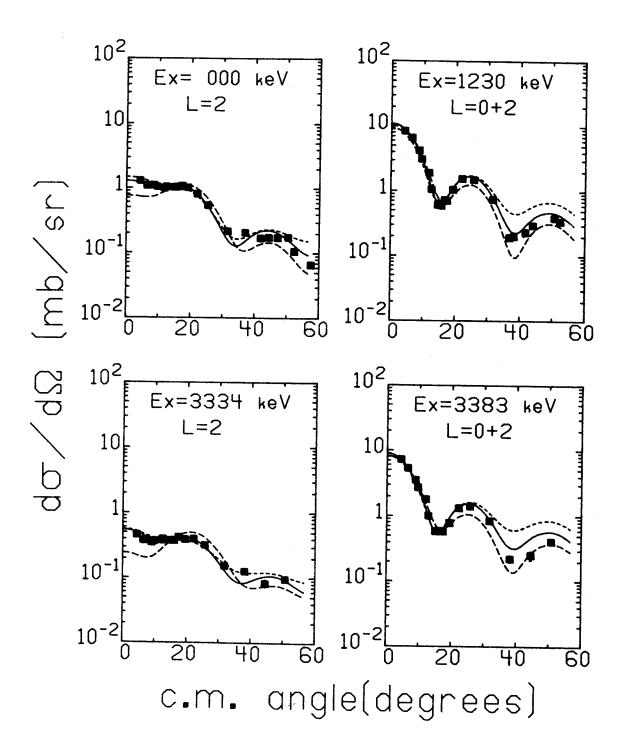


Figure 8

II.4. Discussion of Results

II.4.A. Levels of ²²Na

Experimental evidence on the energies, spins, parities, and other properties of levels in 22Na has been accumulated principally at Brookhaven (see the literature cited in Ref. 9) via studies of the gamma-ray decays of these levels, and at the University of Pennsylvania via charged particle transfer studies. These works have resulted in precise excitation energy assignments to all of these low-lying levels plus some higher excited states, and a rather complete catalog of what levels exist up through 6 MeV excitation. With the (p,d) reaction at 35 MeV, we observe evidence for the existence of all but 2 of the 38 previously identified levels below 6 MeV excitation in 22 Na (see Table 1). The two unobserved levels are very weakly excited in analogous reactions. We observe one new level, at 5.719 MeV, unresolved in previous work. Our assigned excitation energy values agree with previous assignments to within the 1-2 keV combined uncertainties up through 4 MeV excitation. Between 4 and 5 MeV, agreement in excitation energies between the present and previous results is still good, although uncertainties and deviations are both in the 2-4 keV range for that region. From 5 to 6 MeV, there are some significant discrepancies between the present assignments and previous values, which, in this region, have all resulted from

magnetic analysis of charged particle reactions. These discrepancies seem to involve spacings between levels rather than more understandable systematic deviations of scale.

The present assignments (Table 1) for the ℓ -values of the various transitions are, in all cases, consistent with the consensus assignments of J^{π} and with the results of the analysis of $^{23}\text{Na}(^{3}\text{He},^{4}\text{He})^{22}\text{Na data.}^{10}$ The relative values for spectroscopic factors extracted from the present data agree qualitatively with the numbers obtained from the (3He,4He) work. However, the failure to obtain a good l=0 fit to the data with the present DWBA calculations leaves a large uncertainty in our values for C^2S ($\ell=0$). There are some individual deviations between present and previous spectroscopic factors, such as the different ratios of the strengths of the first 3⁺ state to the first 4⁺ state, which might indicate some differences either in the behavior of the DWBA for these two kinds of reactions or in which alternate reaction mechanism is the most significant contributor to the direct single-step process. The results of the analysis of (p,d) data taken at 17.5 MeV for the lowest few states 35 are also consistent with the present analysis.

The observed features of the positive-parity levels of ²²Na, as regards electromagnetic decay and single-nucleon transfer population, have been extensively interpreted in the framework of the Nilsson model. ^{10,36} The most detailed

shell-model analysis of this system, 4 carried out with complete consistency for the A=19, 20, 21, and 22 systems, treats all of the same observables with a uniformly higher degree of success. The spectroscopic factors predicted for 23 Na $^{+22}$ Na transitions are listed in Table 1. The shell-model predictions agree with the experimental results for spectroscopic factors within reasonable uncertainties for the first six states. The $\ell=0$ spectroscopic factor for the first 2^+ , T=1 state, predicted to be C^2 S=0.07, is observed to be less than 0.01. Even though the magnitudes are rather small, this might be an important clue to a failing of the wave functions involved. Larger $\ell=2$ spectroscopic factors are predicted for the second and third 3^+ states than are observed, in particular for the third, at 2.968 MeV excitation.

II.4.B. Results for 34Cl

The energies of the levels in ³⁴Cl have been assigned by a combination of gamma-ray decay and single nucleon stripping experiments. The combined uncertainties of the two kinds of experiments are such that unique identification of states above 3.5 MeV excitation is not always possible. We present in Table 2 a composite of the results of these previous experiments, but do not attempt to quote errors. The uncertainties in the energies of levels below 3.5 MeV are all based on gamma ray measurements and should be good to the order of a kilovolt, or better.

The level energies extracted from the analysis of our data, and their assigned uncertainties, are in agreement with the existing values up through 3.5 MeV excitation. largest deviation, 3 keV, occurs for the "3129" keV state. All levels previously well established to lie in the 0.0-3.5 MeV region are seen in the present data. The level located by Erskine, et al. 17 at 1924 keV, and not seen in any other work, is not observed here. Nonetheless, its existance is not implausible in the context of theoretical spectra for 34cl. which predict a few low-lying levels with vanishing spectroscopic factors. Above 3.5 MeV we fail to observe several states seen in previous work. All of these levels would be expected to be weakly populated via pick-up. This, together with the high density of peaks in this region, makes observation of these levels at enough angles to insure unambiguous identification difficult. At the same time, we excite several levels in the 3.5-5.0 MeV region which have not been previously reported. Most of these are also weakly excited, but a few have significant strengths and are hence of special interest in the present spectroscopic picture.

The third 2^+ and the first 1^+ levels are known to lie close to 4.1 MeV excitation in 34 S (see Table 2) and should occur at about the same energy in 34 Cl. All theoretical calculations predict a significant $\ell=2$ pick-up spectroscopic factor for this 2^+ and a strong $\ell=0$ strength for the 1^+ . The

"level" we observe at 4217 keV has both of these properties. The 1⁺ and 2⁺ levels in 34 S are separated by 43 keV, the 1⁺ lying lower. The first two 2⁺, T=1 states in 34 Cl are raised in excitation energy relative to their positions in 34 S by 32 and 78 keV, respectively. The second of these levels has three times the $\ell=0$ pick-up strength of the first, and we may consider it, crudely, as a $\frac{1}{1/2}d_{3/2}^3$ state relative to the $\frac{d^2}{3/2}$ nature of the first 2⁺ level. The difference in energy shift is quite probably associated with this empirically established difference in the wave functions.

The first 1^+ , T=1 state should be $(s_{1/2}^{-1}d_{3/2}^3)$ in nature All structure calculations agree on this point, and the stripping data in consistent, though not confirmatory, with these predictions. The third 2⁺ level is empirically determined to be mainly $d_{3/2}^2$ in character. Thus, if the energy shifts observed for the lowest two 2⁺ states were to be replicated by the third 2⁺ and the first 1⁺, the 1⁺ level would move up by 46 keV more than the 2⁺. This difference would almost exactly cancel out the 43 keV gap between the corresponding states in '34'S. Hence, the very close degeneracy of these levels in 34Cl would not be a completely unreasonable possibility. However, it must be noted that the total shift of these levels, which must occur if they together form the 4.217 MeV peak, is greater than that observed for the lower two excited T=1 states. Nonetheless, if this peak is not a doublet we have a rather clear-cut discrepancy with theory on our hands as regards spectroscopic factors.

The excited 0⁺, T=1 states, populated strongly via the $^{36}\mathrm{Ar}\,(\mathrm{p},^{3}\mathrm{He})^{34}\mathrm{Cl}$ reaction, should be very weakly populated in the present single nucleon pick-up experiment. We have tentatively assigned the 3942 keV state as 0⁺, T=1, but this is based solely on energy proximity. Likewise, we associate some of the other T=1 states observed in $^{34}\mathrm{S}$ with levels we observed in the 4-5 MeV region. We do not believe that either of the two strongly excited levels at 5 MeV excitation (4998 and 5008 keV is the third 0⁺, T=1 state, but suggest the 4975 keV level as a possibility.

The &-values we assign are all consistent with the consensus spin assignments and stripping &-values. Our results are in repeated disagreement with the previous neutron pickup study 22 as regards dominant &-value assignments and spectroscopic factors for all but the most trivial cases in the low-lying spectrum. Results are compared in Table 2. At higher energies, the lack of adequate resolution in the previous work resulted in a failure to realize several doublets, such as those at 3334 and 3383 keV, and at 4998 and 5008 keV. It should also be noted, parenthetically, that the comparison between experiment and theory in Ref. 22 is further vitiated by an inconsistent treatment of the isospin coupling factor.

There are striking similarities between the $(sd)^{-6}$ -configuration spectrum of 34 Cl and the $(sd)^{6}$ -configuration spectrum of 22 Na. Despite the formal theoretical identity and the resemblance of the sequences of the first few levels,

it must be remembered that the single particle energies and the Pauli Principle limits on orbital occupation dictate that states in $^{22}{\rm Na}$ are dominantly formed out of $\rm d_{5/2}$ configurations while the features of the low-lying levels of $^{34}{\rm Cl}$ arise from some mixture of $\rm d_{3/2}$ and $\rm s_{1/2}$ couplings. The first step to understanding the structure of these latter levels is to determine the way in which $\rm s_{1/2}$ and $\rm d_{3/2}$ particles contribute to each of the individual wave functions.

The two kinds of reactions which most directly relate to this issue are single-nucleon stripping from 33 S and one nucleon pick-up from 35 Cl. The (3 He,d) and (d,p) reactions 17,26 on 33 S have been studied with good energy resolution.

The results of the ℓ -value assignments from these works are noted in Table 2. If a simple $d_{3/2}^1$ model is assumed for 33 S, the measured stripping spectroscopic factors indicate that the " $d_{3/2}^2$ " states of J^π , $T = 0^+$,1, 3^+ ,0, and 1^+ ,0 are the ground, first, and third excited states, with the 1^+ strength being slightly fragmented into neighboring 1^+ levels. The $(d_{3/2}^2)$ 2^+ ,1 configuration seems to be spread over the 2158 and 3383 states in a ratio of about 2 to 1. Many of the levels show some $\ell=0$ strength, indicating a significant lack of closure in the $s_{1/2}$ orbit. A much more realistic shell-model treatment, allowing all three s-d shell orbitals to be active, accounts for a large portion of the details of the stripping results (see Ref. 3, FPSDI Hamiltonian results).

If we assume the simplest model, $(d_{3/2}^3)$, for the 35 Cl ground state, then the present pick-up results express the following qualitative picture. Again, the 0^+ ,1 and 3^+ ,0 states resemble $(d_{3/2}^2)$ states. The $(d_{3/2}^2)$ configuration is spread almost equally over the first three 1^+ ,0 states and is again split between the 2^+ ,1 states at 2.158 and 3.383 MeV. This time, however, the ratio is 1 to 2. The dominant impression yielded by the spectroscopic factor results is, however, one of complexity. Simple shell-model pictures are only faintly suggestive of the complex structure of the low-lying levels revealed in pick-up and stripping. This detailed structure observed in pick-up is also, however, quite well reproduced by the same three-orbit shell-model calculation just mentioned.

The predictions this calculation yields for pick-up spectroscopic factors for the levels of ³⁴Cl are presented in Table 2 for comparison with the experimental results. The correspondences between the lowest eight or so states, and for a few selected higher levels, are quite good. This, together with the almost comparable success obtained for stripping, indicates that the complex shell-model wave functions for these levels have many of the properties required of a realistic and thorough description of the physical states. There are several discrepancies between theory and experiment for higher-lying states. The lack of spin assignments for some of these higher states prevents a more definitive critique of the model results. In Table 2 we have therefore entered

some theoretical states which have significant spectroscopic factors and appropriate energies in line with states of un-known spin.

The spectroscopic factor predictions from this shell-model calculation are actually more successful than are the predictions for energies. There are some inversions in level orderings and a serious compression of the theoretical spectrum. These features, as well as the spectroscopic factor failings at higher excitations, clearly indicate the need for still better calculations. The present experimental results verify, however, that the present calculations form a secure foundation upon which more advanced theoretical work may be based.

II.5. Conclusions

The DWBA analysis of the 35 Cl(p,d) 34 Cl transitions yields good fits to the angular distributions and stable spectroscopic factors. The 23 Na(p,d) 22 Na data is not fit so well. In particular, no formulation of parameters and adjustments we attempted yielded an acceptable $\ell=0$ shape for Na while preserving a reasonable $\ell=2$ prediction for Na and simultaneous good fits to the Cl data.

The spectroscopic factors extracted from the data are well reproduced by recent shell model calculations in the domain of approximately the lowest 10 levels. The spectroscopic

factors also facilitate identification of T=1 levels by comparison with $^{35}\text{Cl}(d,^{3}\text{He})^{34}\text{S}$ results. Several strongly populated states still remain without a unique spin assignment, and when these are fixed, the final combined experimental picture of ^{34}Cl will offer a challenging and hopefully rewarding problem to structure theorists.

III. THE ³⁷Cl(p,d) ³⁶Cl REACTION

III.1. Introductory Remarks

The simplest shell-model description of 36Cl arises from the couplings of three $d_{3/2}$ neutrons and one $d_{3/2}$ proton. obvious model extension is the inclusion of $s_{1/2}$ excitations. 56-58 Recently, the set of configuration basis states has been further expanded to include the $1d_{5/2}$, as well as the $2s_{1/2}$, and $1d_{3/2}$ orbits, 3,59 and initial calculations involving excitations to the f-p shell have also been made for various s-d shell nuclei. 60-61 Several residual interactions and model Hamiltonians have been used in the recent studies, yielding different results for some predicted observables. There is an obvious need for accurately determined experimental quantities in any attempt to critically evaluate, and suggest improvements for, these various models. Since calculated spectra for the odd-even and doubly-even s-d shell nuclei show good correspondence with available data while predictions for the odd-odd nuclei are often in qualitative disagreement with experiment, sound experimental knowledge of the doubly-odd systems is essential to a useful critique of recent theoretical studies.

Although many levels have been previously observed in ³⁶Cl, excitation energies have not been assigned to high accuracy and the spins of several low-lying levels are not as yet unambiguously determined. Only a few single-neutron

pick-up experiments leading to states in 36Cl have been performed. 22,62-65 Spectroscopic information is consequently sparse, with the bulk of the experimental spectroscopic factors available for the strongly populated positive parity levels below 4 MeV excitation and only one negative parity state. The present work is a continuation of a comprehensive study of doubly-odd s-d shell systems via the (p,d) reaction at 35 MeV. 6-8 We have attempted to observe and catalogue as many levels in 36 Cl as possible, assigning them precise excitation energies and extracting spectroscopic factors for the neutron transfers which populate them. Deuteron spectra recorded on nuclear emulsion plates with a total energy resolution of 10-18 keV, FWHM, allowed the assignment of excitation energies in ³⁶Cl to ~8.2 MeV with an overall accuracy of ≤1 keV/MeV. Angular distributions for states up to 8.2 MeV have been taken over a 3° to 55° range, with spectroscopic factors extracted and 1-values assigned for transitions producing analyzable distribution patterns. The forwardangle data allowed essentially parameter-free \$\ell=0\$ spectroscopic factor extraction and a critical test of theoretical &=2 shapes. The present results will be compared with previous experimental works, and their implications for theoretical studies in the upper s-d shell will be discussed.

III.2. Experimental Procedure

Targets for the present experiment were made by evaporating a sodium-chloride compound (enriched to 96.5% in the 37 Cl isotope) onto 30 μ gm/cm² carbon foil backings. The targets were kept under vacuum. Consequently, target thicknesses (20-120 μ gm/cm²) were estimated from deuteron yields and assumed scattering chamber geometry. 35 MeV protons from the Michigan State University sector-focussed cyclotron were used to induce the (p,d) reaction leading to states in 36 Cl and 22 Na. Reaction products were analyzed in the MSU split-pole magnetic spectrograph, deuteron spectra being recorded both with a single-wire proportional counter 32 and on 25 micron thick nuclear emulsion plates.

Spectra were recorded with the counter at closely spaced laboratory angles from 3° to 55° with a total resolution of 50 keV, FWHM. The spectrograph acceptance aperature was 0.6 msr for the angular region of greatest importance (3° to 30°) and 1.4 msr for angles greater than 30°. Data acquisition and particle identification is this portion of the experiment were accomplished in the MSU Sigma-7 computer. These data allowed extraction of complete angular distributions for the levels in ³⁶Cl below 2 MeV excitation. The ³⁷Cl(p,d) ³⁶Cl and ²³Na(p,d) ²²Na Q-values ³⁴ dictate an overlap of their separate deuteron spectra for excitations greater than approximately 2 MeV in ³⁶Cl. Consequently, for higher

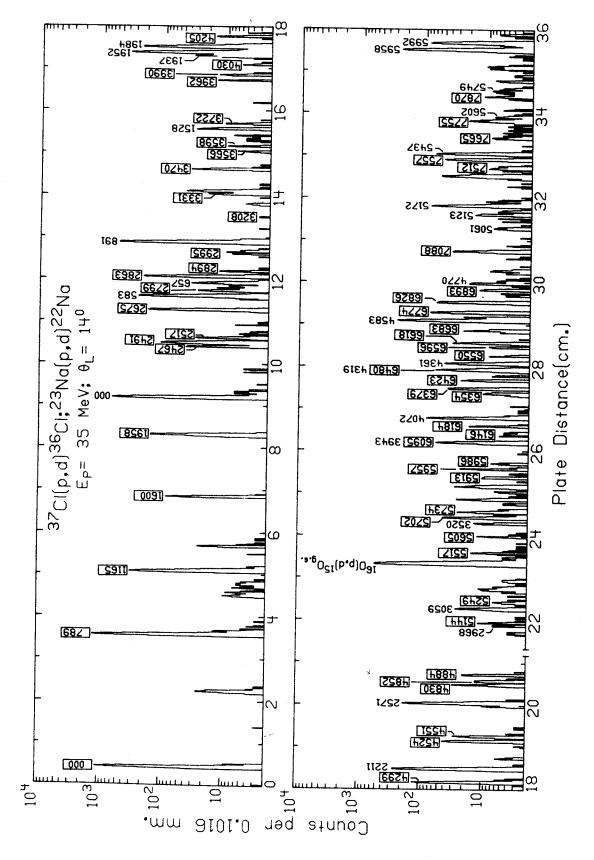
excitations the counter data generally provided useable cross-section measurements only for those 36 Cl levels separated from others in 36 Cl, and from any in 22 Na, by more than the deuteron peak resolution.

Protons elastically scattered from 37 Cl and 23 Na were observed in an experimental configuration identical to that used in the (p,d) measurements, except for an appropriate adjustment of the spectrograph magnetic field. $^{37}\text{Cl}(p,p_0)^{37}\text{Cl}$ and $^{23}\text{Na}(p,p_0)^{23}\text{Na}$ data were recorded at laboratory angles from 25° to 50°, and assumed to have the values predicted by optical-model calculations using the Becchetti-Greenlees proton parameters 37 (see Table 6 and Appendix B). Normalization for the (p,d) data was made relative to these elastic cross-sections. A total uncertainty of 15% is assumed to arise from uncorrelated 10% uncertainties in the optical-model predictions and the normalization procedure itself. The ²³Na(p,d) ²²Na angular distributions observed in this experiment show complete consistency in both shape and absolute magnitude with those obtained in another, independent study at this laboratory. 7 When peaks from the ³⁷Cl and ²³Na reactions coincided, the cross-section associated with the transition to a 36Cl level was, therefore, deduced by subtraction of the independently measured ²³Na(p.d) ²²Na cross-section for the appropriate energy level and angle. Similar corrections for those cases where levels

in 34 Cl, strongly populated via 35 Cl(p,d) 34 Cl, coincided with those in 36 Cl were made after an appropriate consideration of the enrichment factor.

Deuteron spectra were also recorded at angles from 4° to 45° on nuclear emulsion plates. Various runs yielded total particle group resolutions of 10 to 18 keV, FWHM. An example of the best resolution spectra is shown in Fig. 9. The spectrograph acceptance apertures were the same as those used in recording the counter data. The plates were shielded from ${}^{3}\text{He}$ and ${}^{4}\text{He}$ particles by 10 mil Mylar strips and levels in ³⁶Cl to approximately 8.2 MeV excitation were observed. At each angle, the deuteron spectrum to roughly 4.8 MeV excitation in ³⁶Cl was recorded on one 10 inch long emulsion plate, with the remainder of the deuteron groups and the proton groups from scattering on ¹²C, ¹⁶O, ²³Na, and ³⁷Cl falling on a second, abutting plate. Elastic proton spectra recorded with a NaI monitor detector at 90° to the beam, and a beamcurrent integrator were used to achieve relative normalization of all proton and deuteron spectra. Normalization of the plate data to the counter data was accomplished by crosssection comparisons for selected low-lying levels in 36cl and ²³Na at several forward angles.

Figure 9. A spectrum from the (p,d) reaction on the ²³Na-³⁷Cl target, measured at 35 MeV and 14°, as recorded on nuclear emulsion plates. The resolution of the deuteron groups is 10 keV, FWHM. All excitation energy values are from the present work, with those "boxed" indicating levels in ³⁶Cl.



igure 9

III.3. Excitation Energies

Excitation energy analysis and assignments were made on the basis of centroids extracted from the best resolution nuclear emulsion spectra recorded at 4° , 8° , and 14° . The energy levels in 36 Cl presented in Table 5 are a weighted average of the results of two analyses involving these data.

The first method involved much the same procedure used in the analysis of the 39 K(p,d) 38 K reaction. The low-lying excitation energies in ³⁶Cl have not been reported to 1 keV accuracy. Consequently, any energy calibration in the present work must rely heavily on the precisely determined energies in 22_{Na.66} The energy analysis involved a fit to these and other reference energies via a least-squares adjustment of the beam energy, scattering angle, and the constant, linear and quadratic coefficients of a Bo vs. focal-plane-position relationship 67 for the 8° and 14° spectra (see APPENDIX A). At angles <80, effective use of this fitting procedure is greatly hindered by the overlap of all elastic proton levels on the nuclear emulsions. The second plate was assumed to be directly adjacent to the first. Table 4 displays the reference peaks chosen. These levels were used only where accurate, unambiguous centroids could be extracted. Appropriate target loss corrections were made for all reference levels. The best overall results were obtained

Table 4. States used for the energy calibration of the $^{37}\text{Cl}(p,d)^{36}\text{Cl}$ reaction data. Some energies in ^{22}Na extracted in the present work and in a previous (p,d) study are shown to illustrate calibration consistency.

Reaction	Excitation Energy (keV) in the Residual Nucleus ^a	Levels in ²² Na(keV) from previous work ^b	Levels in ²² Na(keV) from this work
	ground state ^C ground_state ^C 583.05+0.1d 657.0+0.14d 890.89+0.2d 1951.8+0.3d 1983.5+0.5d 2211.4+0.32d 2571.5+0.3d 2968.6+0.6d 3059.4+0.6d	000 583+1 657+1 891+1 1952+1 1984+1 2211+1 2571+1 2968+1 3943+2 4072+2 4583+2 5958+4 5992-4	000 + 583 + 1 658 + 1 890 + 1 1952 + 2 1984 + 2 2211 + 2 2211 + 2 2571 + 2 2971 + 4 3061 + 4 4072 + 4 4581 + 4 5959 + 5 5993 - 5
160(p,d)150 12C(p,d)11C 37C1(p,p)37 23Na(p,p)23Na 160(p,p)160 12C(p,p)1C	ground state ground state ground state ground state 441.0 -1.00 ground state ground state		

^aUsed for present calibration.

b See Sec. II.2.

CAdjusted as described in text.

dReference 66.

eReference 68.

when the mass table Q-values for the ²³Na(p,d)²²Na and ³⁷Cl(p,d)³⁶Cl reactions³⁴ were manually adjusted by -2 and -1 keV, respectively. This is consistent with the adjustment of the ²³Na(p,d)²²Na Q-value required in the analysis of ³⁵Cl(p,d)³⁴Cl data (see Sec. II.2.) and within the Q-value errors quoted in the latest mass tables for both reactions. The corrections to the nominal beam energy required by the fit for both angles was +9 keV, with scattering angle corrections <0.3° in both cases. These changes are within the accuracy to which the experimental apparatus and analysis systems yield precise experimental parameters for any given run.

In an effort to obtain the best possible overall excitation energies from the present data, a second fitting procedure was employed for the 4°, 8°, and 14° spectra. The beam energy and scattering angle corrections and the geometrical calibration parameters found in the above analysis were used for the 8° and 14° spectra. Close approximations to these parameters were used for the 4° spectrum since the experimental configuration was essentially the same. This time, a linear, least-squares fit to the deuteron momenta for appropriate reference levels in ³⁶Cl and ²²Na (see APPENDIX A and Table 4) was required. Again, the appropriate Q-value and target loss corrections were made. The excitation energies shown in Table 5 are an average of the results of these two calibration procedures. The errors quoted

include jitter arising from the two calibration methods employed and estimated systematic errors.

Table 4 also indicates some excitation energies in ²²Na returned in the present study, and a comparison with those found from a previous investigation via the (p,d) reaction (Sec. II.2.). The overall consistency in the energy calibration schemes is clearly evident and, consequently, there was little motivation to alter the previous ²²Na excitation energy assignments based on the ²³Na(p,d) ²²Na reaction. Therefore, all ²²Na energies shown in Fig. 9 are those assigned in Sec. II.2.

III.4. Angular Distributions

III.4.A. General Discussion

All orbital angular momentum quantum numbers (ℓ) for the transferred neutrons and corresponding spectroscopic factors have been assigned to transitions observed in the present work on the basis of fits to distorted-wave Born approximation (DWBA) angular distributions calculated using the computer code DWUCK. The optical model potentials are of the standard form:

$$U(r) = V_{R}f(r_{R}, a_{R}) + i(W_{V}f(r_{V}, a_{V}) - 4W_{SF}a_{SF} \frac{d}{dr} f(r_{SF}, a_{SF}))$$

$$+ (\frac{h}{m_{\pi}c})^{2} V_{SO} \frac{1}{r} \frac{d}{dr} f(r_{SO}, a_{SO})^{-\frac{1}{k} \cdot \frac{1}{\sigma}}$$

Table 5. Energy levels in ^{36}Cl observed in the present study and in other works.

				on Energ	-			
(p,d)a	(d,p)b	(n,γ) ^c	$(n,\gamma)^d$	(n,γ) ^e	$(^3 \text{He}, \alpha)^f$	(³ He,α) ^g	(p,d)h	(p,d)
000	000	000	000	000	000	000	000	000
789 ± 1		790	790 * 2	788	78(0)	793 - 15	780-15	787
1165-1	1163+4	1166	1167-2	1165	116(0)	1165-15		
1600 ± 1	1599 [±] 5	1608	1605 [±] 4	1599	160(0)	1608-15	1600-15	
				1951				
1958-1	1954-5	1962	1959 * 3	1959	196(0)	1970+15	1950 * 15	1956
		2164						
		2316						
2467-2	2472 [±] 6	2472	2472-3	2469				
2491-2	2497 - 6				250(0)	2497-15		2490
2517-2	2522-6							
		2617						
2675 [±] 1	2679 * 6	2683	2675-5		268(0)	2682 ⁺ 15		2673
2799 * 3	2816-6							1070
2863 [±] 1	2868-6	2867	2865-3		287(0)	2905 [±] 15		2858
2894-2						20		2000
2995-2	3000-6	2999	2979±5					
		3065	3061±5					
	3103-7		0001					
3208±4	3212-8							
3331 [±] 2	3338+6	3336						
3470±2	3474 ⁺ 7				350(0)	3492-25		04.70
3566±4	• ,	3564			330(0)	3432-23		3477
3598±3	3606 [±] 7	3601						
	3640 [±] 6	3636						
(3661)	3670-8	0000						
3722±3	3728-7				374(0)	3736 - 25		
	(3831)	3822			3/4(0)	3/30-23		
	(3034)	3852						
3962±3	3970 [±] 7	3970						
3990±3		3989						
4030-4	4040 + 7	4030						
		4059						
	4146-7	4137						
4205±3	,	4137						
,	(4263)							
4299 [±] 2	(4300)				433(0)	4333 [±] 25		4297
4316-3	4323-7				100(0)	4000-20		4231
	4413-8							
		4445						
	4504-7	4497						
+524±3		4526						
551-3	4560±8	4560			452(0)	4560 [±] 25		
	4607±8	4601			452(0)	4560-25 4590-25		
	,,,,,,	4618				4590-25		
		4693						
720±3		4033						
738-4	4734-8							
730-4	4765 ⁺ 8	4760				4740±25		
830±4	4834-8							
852-4	4857±8	4838						
884+3	4857-8 4887-8	L 0.7.C						
004-3	4887-8 4919 ⁺ 8	4879			490(0)	4940±25		
953±4	4919-8 4965 - 8	1.070						
333*4	4965-8 5008 [±] 8	4972						
		5009						
144-5	5090±8 5160±8	5156						
144-2		5150						
	5213 ±8	5194						
		5231						

			Excitat	ion Ener	gy (keV)			
(p,d) ^a	(d,p) ^b	(n, _y) ^c	(n,y) ^d	(n,γ) ^e	(³ He, ₀) ^f	(³ He,a) ^g	(b,q)	(p,d) ⁱ
5249-4	5269-8	5250						
	5314-8							
	5339 * 8							
	5376 * 8							
	5469±8							
5517-4		5510						
	5550+8							
	5584+8							
	5622 * 8							
	5701 [±] 8							
5734 - 5	5731±8					5730 [±] 25		
	5766±8				576(0)			
	5836-8							
5913 [±] 4	5871 [±] 8 5906 [±] 8							
5913-4 5957 * 4								
595/-4 5986 - 4	5952-8 5972-8					6000 [±] 25		
5986-4	5972-8 6032-8					6000-25		
6095±4	6090-8							
6146 ⁺ 5	6155±8					6150 [±] 25		
6184 - 4	0133-0					6190-25		
104-4					625(0)	0130-72		
6354±5	6356-8				023(0)			
6379±4	0000-0							
	6445+8				644(0)	6450 [±] 25		
	6474-8				044(0)	6490 ⁺ 25		
	6510-8					0430-23		
6550 * 5	6546-8				653(0)	6540-25		
6596 + 6						0010-20		
6618 [±] 5								
6683 [±] 4	6680 [±] 8					6680-25		
6750 [±] 5						6750-25		
6774 [±] 5								
6826 - 5					685(0)	6840 [±] 25		
6893 [±] 6		-				6890 [±] 25		
	7007 [±] 8							
7088 [±] 5					708(0)	7090 [±] 25		
7165-6					717(0)	7160-25		
7512 * 5								,
7557 <u>±</u> 5					766(0)	7640 - 25		
7665 <u>+</u> 5								
7755-6								*
7870-6								
8184-6								
	-: -						· · · · · · · · · · · · · · · · · · ·	
Presen	t work.			g _{Re}	f. 63.			
^b Ref. 7	3.			ⁿ Re	f. 22.			The state of the

c_{Ref. 72}. d_{Ref. 70}. iRef. 65; (all levels -20 keV except 4297-10 keV).

eRef. 76. fRef. 64; (±20 keV).

where
$$f(r_i, a_i) = -[1+exp(\frac{r-r_iA^{1/3}}{a_i})].^{-1}$$

 ${
m V_R}$ is the real well depth, while ${
m W_V}$ and ${
m W_{SF}}$ are the volume and surface imaginary well depths, respectively. ${
m V_{SO}}$ is the strength of the spin-orbit potential. A standard, uniformly charged sphere of radius ${
m R_C} = {
m r_C} {
m A}^{1/3}$ was used for the Coulomb potential.

The proton optical model parameters of Becchetti and Greenlees 37 were chosen for use in all DWBA calculations presented here. Use of the parameter set presented by Fricke, et al. 50 had little or no effect on the predicted (p,d) angular distribution shapes. A lack of extensive deuteron elastic scattering data for the appropriate mass region and energy led to a search of the available literature in an effort to find a suitable set of optical-model parameters. Deuteron potentials proposed by Perey and Perey, 53 Newman, et al., 52 Hinterberger, et al., 51 Schwandt and Haeberli, 54 Mermaz, et al., 55 and Cowley, et al. 98 were tested in an effort to reproduce pure $\ell=0$ and $\ell=2$ empirical angular distributions recorded for the (p,d) reaction on several nuclei in the $35 \le A \le 39$ region at $E_D=35$ MeV. $^{6-8}$

This investigation indicated that calculations in the local, zero-range (LZR) approximation for all of the standard deuteron potentials were clearly inferior to the shapes produced when finite-range and non-local corrections (FRNL) were introduced. The standard non-locality parameters 49 0.85 and

and 0.54 were chosen for the proton and deuteron, respectively, while the finite-range parameter 49 for the neutron bound-state was chosen to be 0.621 in all cases. FRNL calculations using the "Set I" parameters of Hinterberger, et al. 51 provided the best overall fits throughout the mass region, although the pure $\ell=0$ fits were found somewhat lacking in the observed Q-dependence and all calculations tended to predict cross-sections significantly greater than the data for $0>35^{\circ}$. In some cases, the superiority of this parameter set was not overwhelming although the usefulness of this potential was most gratifying since it is the most broadly-based deuteron elastic scattering parameter set currently available.

The "adiabatic" deuteron model of Johnson and Soper, 43 used in (p,d) analyses in the oxygen 46,48 and lead 45 regions, was also investigated and found to produce poor forward-angle $\ell=2$ shapes.

The shortcomings of the FRNL calculations were found to be at least partially alleviated with the introduction of a density-dependent damping of the $V_{\rm pn}$ interaction. The damping factor used here and in the other concurrent s-d shell studies via the (p,d) reaction, 7,8 is a general Fermi form

$$F(r) = (1.0-1.845 \rho(r)^{2/3})$$
.

where $\rho(r)=0.17[1+\exp(x)]^{-1}$, $x=(r-r_0A^{1/3})/a$, and " r_0 " and "a" are the radius and diffusivity of the neutron bound-state well.

The normalization factor suggested by nuclear matter considerations ⁶⁹ produces an overall renormalization of the calculated DWBA cross-sections, and has been omitted. A more thorough treatment of this deuteron parameter investigative procedure may be found in Sec. IV.

The present data has been analyzed in detail using: (1) the Hinterberger "Set I" deuteron parameters (FRNL), (2) the same parameter set and calculational approximations as (1) with the aforementioned damping correction to the Vpn interaction (DFRNL), and (3) the adiabatic deuteron prescription in the LZR approximation, henceforth referred to as ADIABATIC. These parameters are shown in Table 6. Angular distributions resulting from these three calculations are compared with each other and with the distributions observed in the present experiment for transitions to four levels in ³⁶Cl in Fig. 10. The virtue of the DFRNL calculations is clearly evident over a wide Q-value range for the present data.

III.4.B. Analysis of Experimental Angular Distributions

DFRNL fits to the angular distributions observed in this study for the population of states in ³⁶Cl via the ³⁷Cl(p,d) ³⁶Cl reaction are shown in Figs. 11, 12, 13, 14, 15, 16, and 17. States observed at an insufficient number of angles to allow plausible &-value assignments are not shown.

Optical-model parameters used in the analysis of the $^{37}\text{Cl}(p,d)^{36}\text{Cl}$ data. 9 Table

av													
	()	r _R (fm)	a _R (fm)	W _V (MeV)	r _V (fm)	a _V (fm)	$^{\Gamma}_{R}$ $^{a}_{R}$ $^{W}_{V}$ $^{\Gamma}_{V}$ $^{a}_{V}$ $^{W}_{SF}$ $^{\Gamma}_{SF}$ $^{a}_{SF}$ $^{V}_{SO}$ $^{\Gamma}_{SO}$ $^{a}_{SO}$ $^{\Gamma}_{SO}$ $^{A}_{SO}$ $^{\Gamma}_{SO}$ $^{A}_{SO}$ $^{\Gamma}_{SO}$	r _{SF} (fm)	a _{SF}	V _{SO}	rso (fm)	aso (fm)	rc (fm)
Proton #6.79	79	1.17 0	.75	17 0.75 5.0		1.32 0.57	4.02	1.32	4.02 1.32 0.57 6.2	6.2	1.01	0.75	1.17
Deuteron 86.73-0.35Ecm (FRNL and DFRNL)	35 E cm	1.25 0.73	.73				13.0	1.25	1.25 0.761 6.0	6.0	1.25	1.25 0.73 1.30	1.30
Deuteron ^C 102.76 ^d (ADIABATIC)	16 ^d	1.17 0	.779	1.60 ^d	1.29	0.603	17 0.779 1.60 ^d 1.29 0.603 16.91 ^d 1.29 0.597 6.2	1.29	0.597	6.2	1.01	1.01 0.75 1.17	1.17
Neutron Adjusted to Bound State match separa- tion energy	d to epara- ergy	1.24 0.65	.65				·			λ=25			1.24

aRef.37.

DRef. 51. CRef. 43; proton and neutron parameters from Reference 37.

dvalues shown are for E_{x} =0.000 MeV only; Q-dependence is as given in Reference 37.

Figure 10. A comparison of fits to representative angular distributions from the ³⁷Cl(p,d)³⁶Cl reaction at 35 MeV with the three chosen types of DWBA calculations. All fits were performed over the angular range from 3° to 35°. The curves are identified as follows: ——DFRNL, ----FRNL, and ———ADIABATIC.

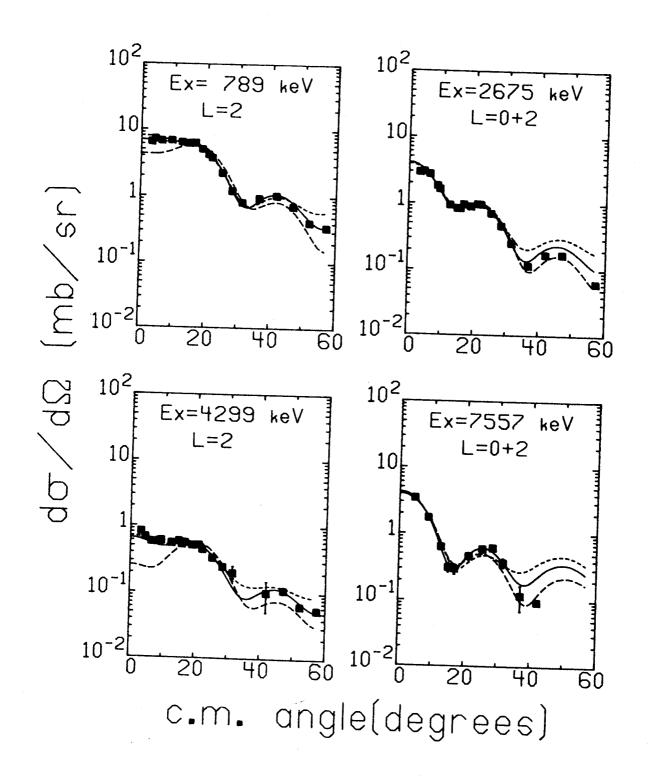


Figure 10

Figure 11. Experimental angular distributions for states in \$^36\text{Cl}\$ as observed in the \$^37\text{Cl}(p,d)\$^36\text{Cl}\$ reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated \$\ell\$-value for mixed-\$\ell\$ distributions.

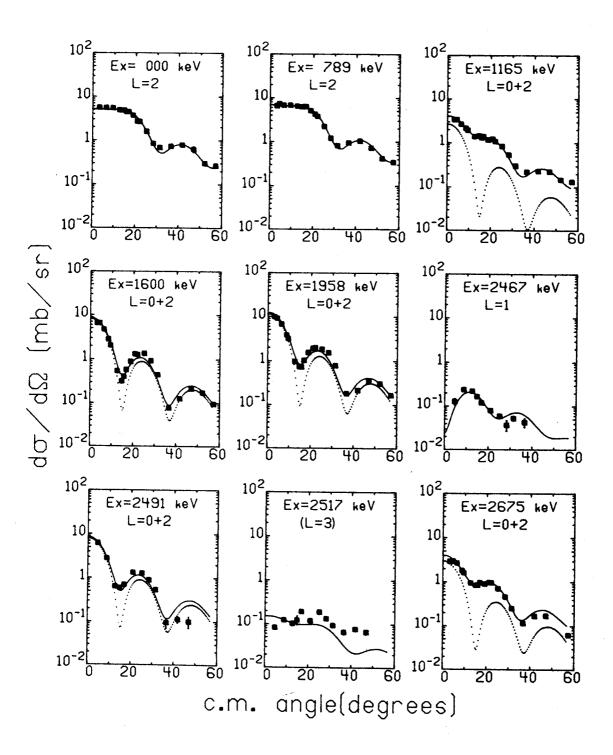


Figure 11

Figure 12. Experimental angular distributions for states in \$^{36}Cl as observed in the \$^{37}Cl(p,d)\$^{36}Cl reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated \$\ell\$-value for mixed-\$\ell\$ distributions.

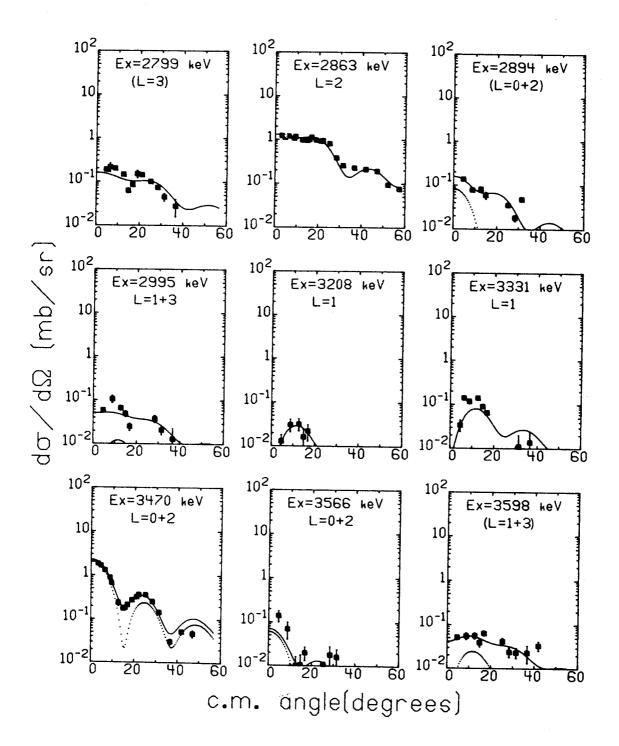


Figure 12

Figure 13. Experimental angular distributions for states in \$^36\text{Cl}\$ as observed in the \$^37\text{Cl}\$ (p,d) \$^36\text{Cl}\$ reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated \$\ell\$-value for mixed-\$\ell\$ distributions.

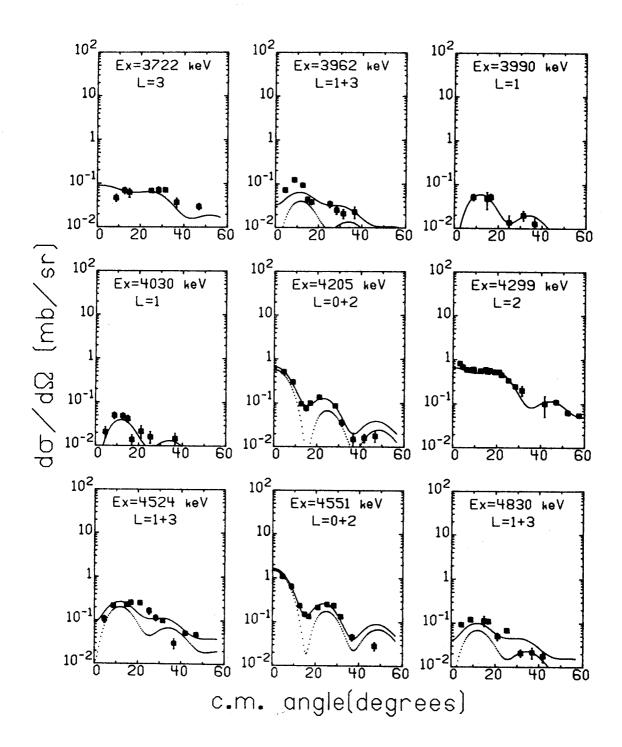


Figure 13

Figure 14. Experimental angular distributions for states in \$^36\text{Cl}\$ as observed in the \$^37\text{Cl}\$ (p,d) \$^36\text{Cl}\$ reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated \$\ell\$-value for mixed-\$\ell\$ distributions.

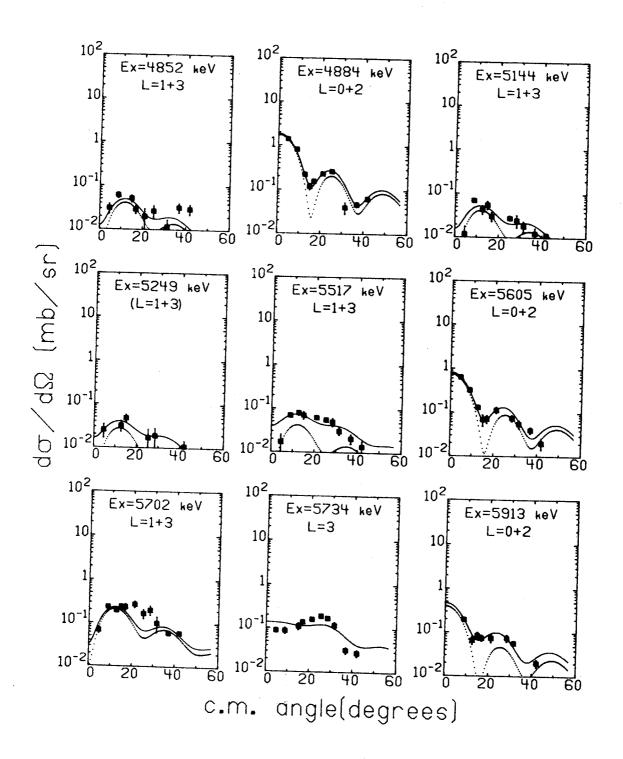


Figure 14

Figure 15. Experimental angular distributions for states in \$^{36}Cl as observed in the \$^{37}Cl(p,d) 36 Cl reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 35°. The dotted curves show the contribution of the first indicated \$\ell\$-value for mixed-\$\ell\$ distributions.

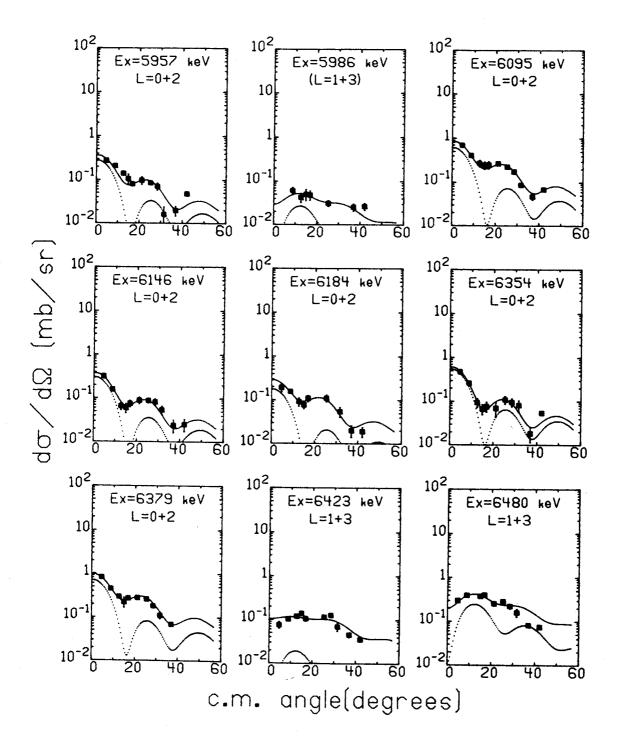


Figure 15

Figure 16. Experimental angular distributions for states in ³⁶Cl as observed in the ³⁷Cl(p,d) ³⁶Cl reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated &-value for mixed-& distributions.

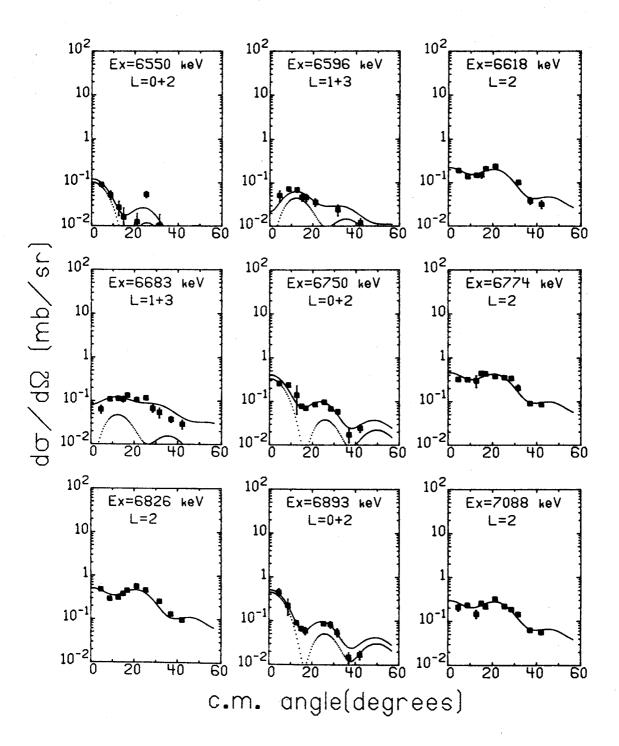


Figure 16

Figure 17. Experimental angular distributions for states in ³⁶Cl as observed in the ³⁷Cl(p,d) ³⁶Cl reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the contribution of the first indicated &-value for mixed-& distributions.

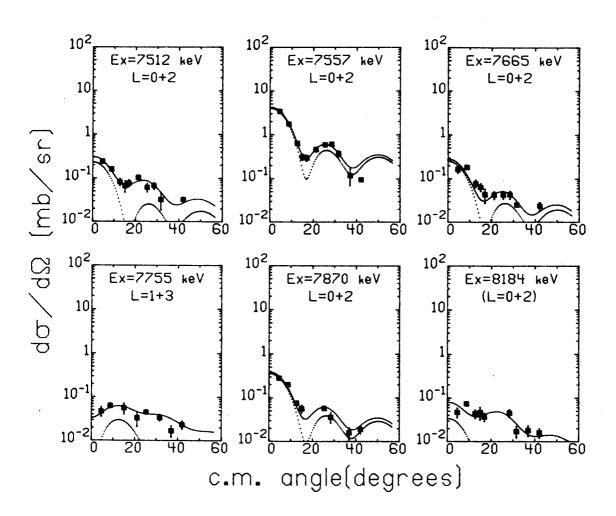


Figure 17

Minimization of the quantity

$$x^{2} = \frac{1}{N} \sum_{i=1}^{N} \left[\left(A_{\ell j} \frac{d\sigma}{d\Omega} \left(\Theta_{i} \right)_{\ell j, DWBA} - \frac{d\sigma}{d\Omega} \left(\Theta_{i} \right)_{exp} \right] / \Delta \sigma_{i}^{2} \right]^{2}$$

where $A_{lj}=2.29~C^2S_{lj}$, with C and S_{lj} the appropriate isospin Clebsch-Gordon coefficient and spectroscopic factor, respectively, was required for all fits. $\frac{d\sigma}{d\Omega}(\theta_i)_{lj,DWBA}, \frac{d\sigma}{d\Omega}(\theta_i)_{exp}$ and $\Delta\sigma_i$ are the DWBA calculated differential cross-section at the ith experimental angle, the experimental value of the differential cross-section at angle i and the total (statistical plus estimated systematic) error in the appropriate experimental number, respectively. N is the number of data points within the $3^{\circ}-35^{\circ}$ angular range. All fits were performed over this subset of experimental points in order to allow comparisons of the resulting spectroscopic factors which are reasonably independent of the great differences found at larger angles for the three calculations used in the present analysis.

Table 7 lists the spectroscopic factors and ℓ -values for all states for which useful angular distributions could be extracted from the present data. Attempts to fit two ℓ j combinations were made for each distribution, except where known final state spins precluded a possible mixed- ℓ transition; for example, the known J^{π} , $T=0^{+}$, 2, 4299 keV level was fit only with a pure ℓ , j=2, 3/2 calculation. In other cases where only one ℓ -value is assigned to a transition, the addition of a

Table 7. Experimental values of ℓ and C^2S_ℓ for the $^{37}\text{Cl}(p,d)^{36}\text{Cl}$ reaction as observed in the present investigation. All assignments are based on the DFRNL analysis, with the spectroscopic factors normalized to yield C^2S_ℓ =1.10 for the transition to the ^{36}Cl ground state.

x(keV)	L	c²sª	E _x (keV)	L	c ² s a
000	2	1.10	5249	(1,3)	<0.01,0.01
789	2	1.66	5517	1,3	<0.01,0.02
1165	0,2	0.05,0.36	5605	0,2	0.02,0.04
1600	0,2	0.16,0.11	5702	1,3	0.02,0.02
1958	0,2	0.23,0.24	5734	3	0.09
2467	1	0.01	5913	0,2	0.01,0.04
2491	0,2	0.17,0.19	5957	0,2	0.01,0.05
2517	(3)	0.05	5986	(1,3)	<0.01,0.02
2675	0,2	0.07,0.31	6095	0,2	0.02,0.15
2799	(3)	0.05	6146	0,2	0.01,0.05
2863	2	0.45	6184	0,2	0.01,0.07
2894	(0,2)	<0.01,0.03	6354	0,2	0.02,0.04
2995	1,3	<0.01,0.01	6379	0,2	0.03,0.18
3208	1	<0.01	6423	1,3	<0.01,0.08
3331	1	0.01	6480	1,3	0.02,0.15
3470	0,2	0.05,0.07	6550	0,2	0.01,0.01
3566	0,2	0.01,0.01	6596	1,3	<0.01,0.02
3598	(1,3)	<0.01,0.02	6618	2	0.15
3722	3	0.04	6683	1,3	<0.01,0.07
3962	1,3	<0.01,0.01	6750	0,2	0.01,0.05
3990	1	<0.01	6774	2	0.31
4030	1	<0.01	6826	2	0.36
4205	0,2	0.01,0.04	6893	0,2	0.02,0.04
4299	2	0.29	7088	2	0.22
4524	1,3	0.01,0.04	7512	0,2	0.01,0.06
4551	0,2	0.04,0.06	7557	0,2	0.18,0.18
4830	1,3	0.01,0.02	7665	0,2	0.01,0.02
4852	1,3	<0.01,0.01	7755	1,3	<0.01,0.04
4884	0,2	0.05,0.05	7870	0,2	0.02,0.02
5144	1,3	<0.01,0.01	8184	(0,2)	<0.01,0.04

^aValues for $\ell=0,1,2,3$ are for $2s_{1/2}$, $2p_{3/2}$, $1d_{3/2}$ and $1f_{7/2}$ calculations, respectively.

second failed to improve the overall fit significantly. In Table 8, a comparison of DFRNL, FRNL, and ADIABATIC results with those of other single neutron pick-up experiments is presented for previously observed transitions only.

III.5. Discussion

III.5.A. Energy Levels

To date, the excitation energies of levels in 36 C1 have not been reported to the precision of states in other s-d shell nuclei. $^{70-77}$ Table 5 serves to illustrate the existing disparity in energy assignments for even the low-lying levels. Nearly all of the levels observed in the $(n_{,Y})$ studies 70 , 71 are observed in the present experiment. We observe only 24 of the 41 levels reported by Alves, et al., 72 but several states not observed in that investigation are reported here and in other single neutron transfer experiments. $^{63-65}$ Much the same situation exists with regard to the $(d_{,P})$ studies of Hoogenboom, et al. 73 and Decowski. 74 The doublet at 1958 keV is not resolved in the present or previous single neutron pick-up works, but the negative-parity state is in all probability very weak, compounding the experimental problem but simplifying interpretation of the resulting "doublet".

The assigned excitation energy of 4299 keV for the 0^+ , T=2 analog of the 36 S ground state agrees very well with the 4297 and 4295 keV assignments of Refs. 65 and 78,

respectively. The energy levels extracted from the present work generally allow a reasonable correlation with those observed in previous studies, particularly for levels below 4 MeV excitation, and many states have been observed for the first time via a single neutron pick-up reaction.

III.5.B. ℓ and π Assignments

Orbital angular momentum quantum numbers (1) for the neutrons transferred in the formation of 61 states in $^{36}\mathrm{Cl}$ via single neutron pick-up can be at least tentatively assigned on the basis of the DFRNL fits to angular distributions observed in the present work. Since the ³⁷Cl ground state is known to have $J^{\pi}=3/2^{+}$, transitions involving even- ℓ transfers populate states in ³⁶Cl with positive parity. Likewise, odd-1 transfers lead to negative parity states. Assignments of £=0+2 were generally evidenced by a definite forward rise in the experimental angular distribution, characteristic of the DWBA $\ell=0$ shape. Separate fits involving $1d_{5/2}$ and $1d_{3/2}$ neutron transfer calculations yielded only slightly different chi-squared per point values over the prescribed angular range for the distributions of positive parity states. Consequently, the 35 positive parity assignments below 8.2 MeV excitation are made on the basis of fits to 1=0 and/or 1=2 DWBA calculations with j=1/2 and j=3/2, respectively.

As a result of the $\ell=2$ spin-orbit splitting for the neutron bound-state, any $\ell=2$, j=3/2 spectroscopic factor may be converted to the appropriate $\ell=2$, j=5/2 value via multiplication by ~ 0.85 .

Transfers involving $\ell=1$ neutrons yield experimental angular distributions with a characteristic "dip" at very forward angles. This is clearly evident in both $lp_{1/2}$ and $2p_{3/2}$ DWBA calculations for this mass region and bombarding energy. As in previous charged particle work 63,73,74 we observe evidence of $\ell=3$ transfers leading to states in 36 Cl. The $1f_{7/2}$ transfer calculations appear somewhat similar to $\ell=2$ DWBA shapes for forward angles but do not fall off as quickly. Therefore, we assign negative parities to 25 levels in ³⁶Cl on the basis of the l=l forward angle fall-off and/or the relatively high $\ell=3$ cross-section around 30°. For all levels, single ℓ -values are assigned when the addition of a second ℓ either resulted in a negative contribution to the cross-section or failed to produce a significant improvement in chi-squared per point values, or when known final state J values excluded mixedtransitions.

The & assignments made on the basis of the present study are shown in Table 7. Parentheses denote levels for which the fit was only slightly preferable to one involving opposite parity &-values. Our parity assignments agree with those made from previous single neutron pick-up experiments, except for

the π =(+) observation for the 5.76 MeV level made by Rosin, et al. 64 We assume a correspondence with the negative parity 5734 keV state observed in this work. The recent 35 Cl(p,d) 36 Cl study by Decowski⁷⁴ assigned at least tentative negative parities to the 2675, 2863, and 2894 keV levels. However, previous pick-up experiments 63-65 have observed positive parity transitions to these levels. The characteristic forward angle $\ell=0$ shape for the 2675 keV state and the excellent $\ell=2$ fit to the 2863 keV level observed in the present work confirm the positive parity assignments to each of these levels and limit their J^{π} values to $(1,2)^{+}$ and $(0-3)^{+}$, respectively. The present data also indicates a rise in cross-section at forward angles for the 2894 keV state, again indicative of a positive parity transition. Also based on the forward angle data, we assign positive parities to the 3470, 5605, 5906, and 6095 keV states as opposed to the π =(-) assignments of Hoogenboom, et al. 73 All other present parity assignments for levels showing reasonable energy correspondences agree with those based on previous (d,p) works.

III.5.C. Experimental C²S Values

In Table 8 we present a comparison of the spectroscopic factors obtained from the DFRNL, FRNL, and ADIABATIC fits and from the previously performed single neutron pick-up experiments leading to states in ³⁶Cl. Only previously observed levels are

for transitions from ³⁷Cl to ³⁶Cl. Absolute values Experimental values of $\mathbb{C}^2 \mathbb{S}_{2}$ Table 8.

Table 8.	Experimer for the g normalize	ment e gr	Experimental values of for the ground state normalized such that	or c e are t C ² S _g	or transitions from presented in parentheses = 1.10 for the ground st	dansicions irom in parentheses the ground st	All ate.	other values are	•	
Ex(kev) ^a	T, T	g a	DFRNL	FRNL	ADIABATIC ^a	q(p,q)	(³ He,ω) ^C	(³ He, ω ^d	(d,t) ^e	(p,d) ^f
			٣.	80	٥.			ε.	0.	6
000	2+1	2	1.10	1,10	1.10	۲.	1.10	1.10	1.10	1.10
789	3+2	7	9	S	9	1.59	10	9.	. 70	9
1165	1+,1	0	0	0	0	۰.	_		٥.	٦.
)) !	 	5	ຕ	ω,	ω.	.	0.35	0.37	. 42	≠.'
1600 (1.	(1,2)+,1	0	4	۲.	۲.	۲,	$\overline{}$	۲.	0	۳,
	•	7	۳.	0	۲.	۲.	2			
1958	2+,1	0	7	7		±.	.37-	0.42	۲.	0.79
)	i •	7	.2	۲.	.	۲.	J. 3		. ⁴²	
2491 (1,	$(1.2)^{+}.1$	0	٦.	.2	٦.	۳,	.32-0.1	0.38	0	
) }		7	٦.	۲.		۲.	.21-0.2			
2675	(1),1	0	0.	٥.	٥.					
)	1 6	7	ິ.	.2	۳.	0.34	0.43	0.37		
2863 (0-	(0-4)+1	0			۰.					
	•	2	≠.	ω.	ⅎ.	0.47	က္	0.38		
3470 (1,	$(1,2)^{+},1$	0	0	0	۰.	•	٠.	۲,		
		7	0.07	0.05	۰.	*0.0 >	0.08			
	$(2-5)^{-1}$	က	0	0	٥.		Τ.	0.05		
1299		7	2	.2	۲,	0.31	ᠴ.	۳,		
	$(1,2)^{+},1$	0	۰.	٥.	۰.		Τ.			
		2	0	٥.	۰.		٠,			
		က	٥.	٥.	٠.		۲.			
	$(0-3)^{+},1$	7	ب	. 2	₹.		⊸.			
7557	2+,2	0	۲.	۲.	٦.					
	•	7	۲.	٥.						

Reference 62. fReference 22. 82=1 h2=2 ^bReference 65. aPresent work. CReference 64. dReference 63. included. Relative to the DFRNL values, the FRNL calculations yield somewhat lower &=2 spectroscopic factors in the &=0+2 mixtures, that disparity increasing with excitation energy. In contrast, the ADIABATIC &=2 values tend to be higher in these mixtures. These deuteron parameter and calculational differences appear to be a direct result of the basic &=0 Q-dependences, i.e., the FRNL and ADIABATIC shapes retain less and more of the first minimum, respectively, with increasing excitation energy.

The DFRNL spectroscopic factors are generally in good agreement with those obtained from previous studies. However, significantly more total strength is assigned to the 1165, 1600, and 1958 keV states by Vignon, et al., 22 and to several of the low-lying levels in the (d,t) study by Puttaswamy and Yntema. 62 The present experiment also allows the observation of mixed $\ell=0$ and $\ell=2$ contributions to several levels for which pure 1=0 or 1=2 transfers have previously been assigned. particularly interesting example is the 2675 keV state. previous pick-up experiments in which this level was ob $served^{63-65}$ assigned a pure $\ell=2$ transfer to the transition. However, the present data for $0<10^{\circ}$, a region not explored in any of those works, definitely indicates the characteristically $\ell{=}0$ forward angle rise (see Fig. 13). The inclusion of an $\ell{=}2$ contribution to several previously assigned pure £=0 transitions seems justified on the basis of DWBA &=0 shape comparisons discussed in Sec. IV.

We observe only one strongly populated positive parity state in the 4 MeV excitation region, with $C^2S_{2,3/2}=0.29$. The $^{37}C1(d,^3He)^{36}S$ work of Gray, et al. 79 and Puttaswamy and Yntema 80 yield values of 0.27 and 0.33, respectively, for the transition to the 0^+ ground state. Therefore, we concur with Refs. 63-65 in the assignment of J^{π} , $T=0^+$, 2 for the 4299 keV level, as the analog of the ^{36}S ground state. The two $(d,^3He)$ works also show considerable spectroscopic strength for the 3.3 MeV, 2^+ level in ^{36}S . The 7557 keV state in $^{36}C1(C^2S(\ell=0)=0.18$, $C^2S(\ell=2)=0.18$) appears to be the most likely candidate for the analog of that level, based on its total strength relative to the other levels observed in that energy region and the spectroscopic factors of $C^2S(\ell=0)=0.22$, and $C^2S(\ell=0)=0.30$ for the 3.3 MeV ^{36}S state reported in Refs. 79 and 80, respectively.

III.5.D. Comparison with Shell-Model Calculations

The spectroscopic factors extracted from the present data (DFRNL) and those calculated from various shell-model Hamiltonians are presented in Table 9. The results of the Tabakin interaction calculations have been renormalized to facilitate a relative comparison with the present results. The MSDI and 12.5 pA studies conducted by Wildenthal, et al. tend to be less successful for upper s-d shell nuclei and have been omitted.

A comparison of $\mathbb{C}^2S(\mathfrak{l})$ values obtained in the present study with those from various shell model calculations. Table 9.

E _x (keV) ^a	T, T	ન જ	C ² S(£)ª	11.0h+ASPE ^b	12.5p+ ¹⁷ 0 ^b	TABAKIN ^C	2-shell ^d
000	2+,1	2	1.10	1.11	1.08	1.10	1.10
789	3,1	7	1.66	1.57	1.52	1.58	1.50
1165	1,1	0	0.05	0.03	0.05	40.0	<0.01
		2	0.36	0.26	1110	0.18	0.27
1600	(1),1	0	0.16	0.13	0.05	60.0	η£*0
		5	0.11	0.14	th0 * 0	0.13	0.05
1958	2,1	0	0.23	90.0	0.28	90.0	0.2
		5	0.20^{f}	0.05e	0.36	0.046	0.02
2491	(2) ⁺ ,1	0	0.17	0.42	0.05		0.50
		5	0.16^{f}	0.16	0.02		90.0
2675	(1),1	0	0.07	00.00	0.01		
		8	0.31	0.14	0.036		0.2
2863	(3),1	7	0.38^{f}	0.50	0.81 ^e		
3470	(1),1	0	0.05	0.23	0.25		
		2	0.07	0.13	0.05		
4299	0, 5	7	0.29	0.22	0.23	0.24	0.22
7557	2,2	0	0.18	0.28	0.27		
		2	0.15^{f}	<0.01 ^e	0.01		0.3
apresent Work, beference 3; are summed for Reference 59 state; all ve for comparison	Present Work. Reference 3; 1d3/2 are summed for k=2 absolutes all values here for comparison; d3/8	/2 and =2 tra solute is have	apresent Work. Dreference 3; 1d3/2 and 1d5/2 contributions are summed for \$\frac{2}{2}\$ transitions. Creference 59; absolute \$C^2\$2=0.85 for ground state; all values have been renormalized for comparison; d3/2 and d5/2 contributions summed for \$\frac{2}{2}\$.		d2s1/2, 1d3/2 calculwave functions of Reported in Reference Predominantly d5/2.	ations eference 64.	using the se 56 re-

Nine T=1 levels have been included in Table 9, with firm spin assignments having been made to four. The other spins have been tentatively assigned on the basis of the neutron orbital angular momentum transfers observed in this work (the presence of $\ell=0$ components limiting final state spins to 1 or 2) and the general trends of recent shellmodel level sequencing. It is evident that the ground state and 789 keV level spectroscopic factors for all of the calculations are in good agreement with present results. is not surprising since, in isospin formalism, the wave functions for these two levels are dominated by a $(d_{5/2})^{12}(s_{1/2})^4(d_{3/2})^4$ configuration, the simplest of shellmodel pictures for 36 Cl. The agreement is also good for the second excited state, although the Tabakin calculations 59 exhibit only about one-half the observed &=2 strength. higher excited states, the predicted spectroscopic factors are very sporadic, with no clear choice of a preferred set of wave functions. However, there is some indication of an over-estimation of the $\ell=2$ strength and the $\ell=0$ strength for transitions to the second 3 level and the fourth 1 level, respectively. The full s-d shell calculations of Wildenthal, et al. 3 predict a weakly populated 3 tlevel near 4 MeV excitation, but no pure l=2 transitions of appropriate strength are observed in that region. A 3⁺ level populated by predominatly $d_{5/2}$ transfer is predicted for the 5-6 MeV

region ($C^2S(\ell=2)=0.2$), which may correspond to the observed 6618 keV level ($C^2S(\ell=2)=0.13$). The only other T=1 state predicted to carry significant pick-up strength is a 4^+ level at approximately 7 MeV excitation ($C^2S(\ell=2)=1.24$). Three levels with significant pure $\ell=2$ strength are observed near 7 MeV (6774, 6826, and 7088 keV) with total $C^2S(\ell=2)=0.77$.

The spectroscopic factors extracted from the present data for the 4299 and 7557 keV levels agree with the 2 and 3 orbital shell-model predictions except for the experimentally observed $\ell=2$ strength of the transition to the latter state. Since they are the only strongly populated levels in the appropriate energy regions and exhibit the correspondingly correct ℓ -values, we concur with previous pick-up works in their identification as the analog states of the $(J^{\pi},T)=(0^{+},2)$ ground state and $(2^{+},2)$ 3.30 MeV levels in 36 S, but assign the excitation energies in 36 Cl much more accurately.

Single-shell sum rules for spectroscopic factors dictate a T=1 contribution to the total $\rm d_{3/2}$ strength of 3.75 with the T=2 levels adding 0.25 for a total $\rm d_{3/2}$ shell-model limit of 4.0. The summed $\rm \ell=2,j=3/2$ spectroscopic strength observed for transitions to the ground state, 789, 1165, 1600, 2675, and 3470 keV levels in $\rm ^{36}Cl$ is 3.61. These states indeed show a majority of the predicted $\rm d_{3/2}$

strength for the T=1 levels in recent shell-model studies. The observed $\ell=2$ spectroscopic factor for the 4299 keV level would indicate that appropriate transitions to that state carry essentially all of the $d_{3/2}$ strength for the A=36,T=2 system. A total $d_{5/2}$ spectroscopic strength of 2.61 may then be assigned to the single neutron transfers to states in 36 Cl below 8.2 MeV, after the $\ell=2$ values in Table 7 have been properly normalized to correspond to $d_{5/2}$ transitions.

Erne 60 has predicted 24 T=1, negative parity levels in 36 Cl between 2.0 and 6.5 MeV excitation. In the present study, 25 levels between 2.0 and 8.2 MeV are assigned at least a tentative negative parity, in excellent agreement with theory. The summed observed spectroscopic strengths are 0.15 and 0.69 for $^{2p}_{3/2}$ and $^{1f}_{7/2}$ neutron transfers, respectively.

III.6. Summary

Excitation energies have been assigned to many levels in 36 Cl with a precision heretofore unmatched in many previous studies of that nucleus. Spectroscopic factors for single neutron pick-up leading to many negative parity states in 36 Cl have been reported for the first time. Essentially all of the $\rm d_{3/2}$ strength and nearly one-half the expected total $\rm d_{5/2}$ transition strength have been observed below 8 MeV

excitation, with the approximate distributions among the T=1 and T=2 levels agreeing well, in total, with recent shell-model calculations. Approximately 60% of the shell-model limit for \$\ell=0\$ strength is also observed in this energy region. The summed negative parity (\$\ell=1,3\$) spectroscopic factors indicate small but significant f-p shell components in the \$^{37}C1 ground state wave function. A level-by-level comparison of the present results with recent predictions indicates a need for the inclusion of f-p shell excitations in any attempt to fully describe the levels in \$^{36}C1 above 2 MeV excitation.

IV. THE 39K(p,d) 38K REACTION

IV.1. Introductory Remarks

In the simplest shell-model picture, the lowest energy states of 38K should arise from the couplings of two d_{3/2} holes, yielding J^{π} , T values of 3^{+} and 1^{+} , T=0, and 0^{+} and 2^{+} , T=1. The incorporation of $s_{1/2}$ -hole excitations into this picture is the most logical first improvement, a step taken by Glaudemans, Wiechers, and Brussaard. 56 Their shell-model provides a description for many aspects of the low-lying positive parity states in ³⁸K. However, much as appears to be the case for the two-particle nucleus in the s-d shell, ¹⁸F, the mixing of the $d_{3/2}$ and $d_{5/2}$ orbits may be important even in the lowest few energy levels. Several calculations which consider excitations in all three s-d shell orbits have been reported, 3,59,81 and appear to yield still further improvement in the agreement between theory and experiment. Finally, again in analogy with ¹⁸F and excitations from the p shell, the structure of $^{38}{\rm K}$ cannot be explained in final detail without recourse to excitations from the s-d shell to the f-p shell. Some initial investigations along these lines have also been reported.

We attempt in the present work to provide an accurate and complete experimental summary of two aspects of the structure of 38 K. The first of these involves making a catalog of as many of the levels in the low-energy region

as possible, and assigning them precise excitation values. To this end, we have measured multiple spectra, using the (p,d) reaction on ³⁹K, with a resolution (10 keV, FWHM) that is at least three times better than that achieved in any of the previous particle-detection work on this nucleus 82,83 and ten times better than that achieved in previous single-neutron transfer experiments 64,84-86 leading to ³⁸K. The second aspect of our study involves measuring the 1-values of the neutron transfers which populate these states, and the associated spectroscopic factors. been done by a carefully cross checked DWBA analysis of the experimental angular distributions of the observed transitions, which were measured all the way in to $\theta_{T}=3^{\circ}$. We will discuss our results in their relation to the previous experimental situation and in their implications for the current theoretical pictures for this and neighboring nuclei.

IV.2. Experimental Procedure

Thin ($\sim 70~\mu gm/cm^2$) targets were made by evaporating natural potassium metal (93% 39 K, 7% 41 K) onto thin carbon backings (30 $\mu gm/cm^2$). These targets were kept under vacuum throughout the experiment and thicknesses were estimated from the (p,d) yields and scattering chamber geometry. The targets were bombarded with 35 MeV protons from the MSU Cyclotron, and reaction products were analyzed in an Enge-type split-pole

magnetic spectrograph. Deuteron spectra were obtained both with a single-wire proportional counter ³² and with 25 micronthick nuclear emulsion plates. The counter data yielded angular distributions at closely spaced angles from 3° to 55° for the strongly populated levels separated from their neighbors by more than the counter resolution of 50 keV, FWHM. The spectrograph acceptance aperture was 0.6 msr for angles than 30° and 1.4 msr for angles greater than 30°. Particle identification and data acquisition in this part of the experiment were accomplished in the MSU Sigma-7 computer.

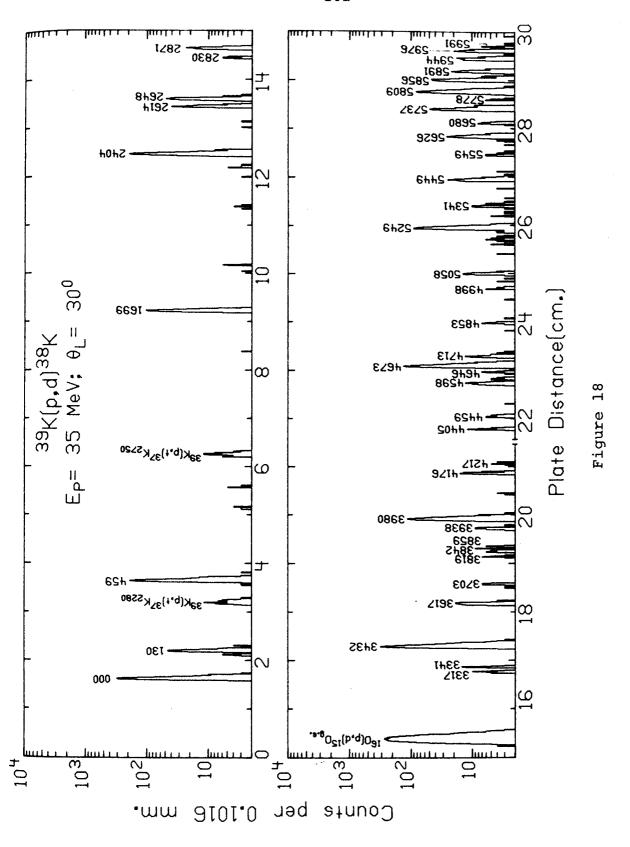
An appropriate change of the spectrograph magnetic field allowed observation of protons elastically scattered from $^{39}{\rm K}$ in an experimental configuration otherwise identical to that used for the (p,d) measurements. Data for $^{39}{\rm K}({\rm p,p_o})^{39}{\rm K}$ were taken at angles from $25^{\rm O}$ to $45^{\rm O}$ and the cross-section normalization for the (p,d) data was taken relative to these elastic cross-sections, after an appropriate adjustment of the measured proton yields accounting for the $7^{\rm k}$ $^{41}{\rm K}$ target contamination. The measured proton elastic scattering cross-sections were assumed to have the values predicted from an optical-model calculation using the Becchetti-Greenlees 37 parameters (see APPENDIX B). We estimate an uncertainty of 10% in the optical model prediction for this mass and angular range, and an additional 10% uncertainty in the mechanics of our normalization procedures.

Spectra were also taken with nuclear emulsions at laboratory angles from 4° to 42°. A typical example is shown in Fig. 18. The average resolution obtained for the deuteron groups here was approximately 10 keV, FWHM. The spectrograph acceptance apertures were the same as those used for the counter data and levels in ³⁸K up to 6 MeV of excitation were recorded. For each angle, the deuteron spectrum to approximately 4.5 MeV was collected on one 25 cm-long emulsion plate, with the remainder of the deuteron groups and the proton groups from scattering on $^{12}\mathrm{C}$, $^{16}\mathrm{O}$, and $^{39}\mathrm{K}$ falling on a second abutting plate. The upper limit of 6 MeV for the energy range presented here was determined by the position of the elastic proton groups at forward angles. Relative normalization of all deuteron and proton spectra was accomplished by the use of a NaI monitor detector which recorded elastic protons scattered at 90° to the beam. A beam-current integrator was also used to check normalization consistency.

IV.3. Excitation Energies

Centroids of the deuteron and proton groups which were used in the analysis and assignment of excitation energies were extracted from the spectra recorded with nuclear emulsions at 14°, 18°, and 20°. The analysis involved the fitting of selected reference peak energies to precisely

Figure 18. A spectrum from the ³⁹K(p,d) ³⁸K reaction, measured at 35 MeV and 30°, as recorded on nuclear emulsion plates. The resolution of the deuteron groups is 10 keV, FWHM. All ³⁸K excitation energy values are from the present work.



known values 34,67,87-89 via a least-squares iteration of the beam energy, the scattering angle, the small gap between the abutting plates, and the parameters appropriate to a quadratic Bp vs. focal-plane-distance relationship. 67 The reference peaks chosen for this analysis (used only at those angles for which they yielded accurate, unambiguous centroids) are shown in Table 10. In all cases, appropriate target-loss corrections were taken into account. We found it impossible to obtain a good fit to the reference energies if we used the accepted ³⁹K(p,d) ³⁸K O-value of -10860^{+}_{-8} keV. ³⁴ An equal-weight, minimum chi-squared fit to all reference peaks was obtained by adjusting this accepted value by +9 keV. This same adjustment was required if all levels from $^{39}\text{K(p,d)}^{38}\text{K}$ except the ground state were omitted from the calibration data set. In all fits, the chi-squaredper-point value was $^{\circ}$ l. The greatest adjustments to the nominal beam energy and scattering angle which the fits required were 8 keV and 0.2°, respectively. These changes are compatible with the accuracy with which we set up the cyclotron beam line and the scattering chamber-spectrograph geometry.

The assignment of any given level to 38 K was made on the basis of a series of angle-to-angle comparisons of measured excitation energy. A level in 40 K (from 41 K(p,d) 40 K) misidentified at 14 0 as belonging to 38 K would, at 20 0 ,

Table 10. States used in the energy calibration for the $$^{39}{\rm K(p,d)}^{38}{\rm K}$$ reaction data.

Reaction	Excitation Energy (keV) in Residual Nucleus
³⁹ K(p,d) ³⁸ K	ground state ^a
	459.6 [±] 1.2 ^b
	1699.4 [±] 1.3 ^b
	2403.8 [±] 1.2 ^b
	2871.0 ⁺ 1.2 ^b
¹⁶ 0(p,d) ¹⁵ 0	ground state ^C
¹² C(p,d) ¹¹ C	ground state ^C
	1.9992 [±] 1.0 ^d
³⁹ K(p,P) ³⁹ K	ground state
	2522.7 ⁺ 0.3 ^e
	3019.3 ⁺ 0.2 ^e
¹⁶ 0(p,p) ¹⁶ 0	ground state
$^{12}C(p,p)^{12}C$	ground state
	4440.0±0.5 ^f

^aAdjusted as described in text.

b Reference 87.

C Reference 34.

d Reference 67.

e Reference 88.

f Reference 89.

show a shift in assigned excitation energy of almost 4 keV because of the incorrect assumption made for the target mass. Shifts of this type, easily observed in the present high resolution data, naturally increase for larger angular differences, lighter nuclei and (p,t) reactions, allowing the unambiguous assignment of the various particle groups to specific residual nuclei.

The present analysis allowed the assignment of excitation energies to several levels in 40 K which fall close to the lowest few levels of 38 K in the spectrograph focal plane. Two of these levels, to which we make assignments of 2258 and 2575 keV, are known to have excitation energy values of 2260.6 $^{+}$ 1.0 keV and 2574.7 $^{+}$ 1.0 keV from Ge-Li detector studies of their gamma ray decays. 90 Since the Q-value for 41 K(p,d) 40 K is known (-7871.3 $^{+}$ 1.4 keV) to good accuracy 34 and our analysis indicates that Q[41 K(p,d) 40 K]-Q[39 K(p,d) 38 K]=2980 $^{+}$ 2 keV, we can assign Q[39 K(p,d) 38 K]=-10851 $^{+}$ 2 keV either on the basis of this "local" comparison, which is essentially independent of the overall focal-plane calibration, or on the basis of the systematic calibration of 50 cm of the focal plane as described above.

The excitation energies we assign to levels of 38 K observed in the present study are presented in Table 11. The results of other studies of 38 K 82 , 83 , 85 - 87 , 91 , 92 , 64 are also presented in this table. It can be seen that almost all levels of 38 K observed in other reactions are found in the present

Table II. Energy levels of ³⁸K excited in the present investigation of the (p,d) reaction and in previous studies of other reactions.

a	h	(H.I.,Y)C	on Energy		σ	.3 .h	.ai
(p,d) ^a	(d,a,Y) ^b	and (β,γ)d	(d,α) ^e	(d,α) ⁺	(d,t) ^g	(³ He,α) ^h	(He,α)
000	000		000	000	000	000	000
130±1	131.4±1.2	130c	144	119	128	138	13(0)
459±1	459.6±1.2		459	43(0)	456	466	45(0)
1699±1	1699.4±1.3		1702	169(0) 241(0)	1704 2405	170(0) 240(0)	170(0) 240(0)
2404±1 2614±2	2403.8±1.2 2514.1±1.4		2403 2624	261(0)	2403	240(0)	240(0)
2648±1	2649.4±1.8	2646 ^C	2024	263(0)	2639	263(0)	264(0)
2830±1	2831.5±1.3	2040		281(0)			
871±1	2871.0±1.2		2864	284(0)		285(0)	287(0)
	2995 ±2		3000	297(0)			
				305(0)			
3317±1	3319 ±2		3327	333(0)			
3341±2	3347 ±3	3337d					
	21.22	3420C	01:4:0	342(0)	21.11.7	342(0)	31111(0)
3432±1	3432 ±2	3458C	3440	344(0)	3441	342(0)	344(0)
3617±1		3436~		360(0)			
01/11	3670 ±2			365(0)			
3703±3	30.0 22		3691	367(0)			
				370(0)			371(0)
3819±2				379(0)			
3842±3				381(0)			
3859±3			3865	383(0)			
3938±2				391(0)	2000	207(0)	400(0)
3980±2			3980	394(0) 414(0)	3989	397(0)	400(0) 420(0)
+176±2 +217±2				418(0)			420(0)
+321±3				410(0)			
+338±3						•	436(0)
4405±3							
4459±3							450(0)
∔59 8 ±2							
+646±3							
+673±2					4660	460(0)	467(0)
4713±3							
4853±3							
4998±3 5058±3							508(0)
5249±3						523(0)	525(0)
5341±3						020(0)	020(0)
5449±2	,					544(0)	545(0)
5549±4							
5626±2						-	562(0)
5680±3							
5737±2							•
5778±4							
5809±3							578(0)
5856±3							585(0)
5 891 ±3						*	
5944±3 5976±3							
5991±3							

aPresent Work.

bReference 87.

CReference 91.

dReference 92 (±10 keV).

eReference 82 (quoted to only the nearest 10 keV).

FReference 83.

gReference 85 (±15 keV).

hReference 86 (quoted to only the nearest 10 keV).

iReference 64 (quoted to only the nearest 10 keV).

work. Below 4 MeV excitation there appear to be six levels observed in $(d,\alpha)^{82,83}$ particle-detection experiments or in $\left(\text{d,}\alpha\right)^{87}$ and heavy-ion initiated 91 gamma-detection experiments which we do not see in the (p,d) spectra. Reasonably sure correspondences can be established between the nineteen levels we do observe in this region and previously reported levels. Of the six levels we do not observe, three are seen by at least two other investigations, while two are reported only by Jänecke⁸³ and one only by Engelbertink.⁹¹ There is reason to think⁹¹ that the 3420 keV and 3458 keV levels have $J \ge 5$, which is consistent with their being very weakly populated via the (p,d) reaction. There are no such simple explanations available for our non-observance of the other four levels. the 4-5 MeV region of excitation Jänecke again reports two or three more levels than we observe, but the discrepancies between his and our energy calibrations make it difficult to be sure which levels are which in that region.

Of the forty-six levels below 6 MeV excitation observed in the present study, only twenty have been observed in the various previous studies of single-nucleon transfer reactions leading to ³⁸K. All of the levels reported in these earlier investigations are observed in the present work.

The excitation energy assignments made in the present study agree well with the results of the most precise previous investigations. 82,87,91,92 The only significant discrepancy is the 6 keV gap between the (p,d) recorded energy of 3341⁺2 keV

and the $(d,\alpha\gamma)$ recorded energy of $3347^{+}_{-}3$ keV. Some of the energies quoted in Ref. 93 differ widely from our values, but these discrepancies are probably not outside the uncertainties, arising from lack of resolution, in that particular study.

The uncertainties quoted for our excitation energies are the total estimated probable errors, compounded from the reproducibility of peak positions inherent in the scanning of the emulsions, uncertainties in the calibration energies, and uncertainties in the details of the spectrograph calibration. They are consistent with the scatter observed in analyzing several different spectra with several variations of the way in which the energy-analysis program is applied. Values of the differences in excitation energy between pairs of states 50 to 1000 keV apart should always be good to 1-2 keV as long as both were populated with reasonable strength.

IV.4. Angular Distributions

IV.4.A. Discussion of DWBA Calculations

The DWBA calculations 49 we discuss here were all made with the proton optical-model parameters of Ref. 37. Although another parameter set 50 produces discernibly different proton elastic scattering predictions for s-d shell nuclei at E_p=35 MeV, the DWBA (p,d) predictions are quite insensitive to the differences between these two proton potentials.

There is a lack of extensive deuteron elastic scattering data for the mass region of the s-d shell at energies appropriate to the present experiment. This necessitated an extensive survey of the relevant literature in an attempt to find a suitable set of such parameters. The criterion of suitability was, of course, a reasonable reproduction of our observed angular distribution shapes. The criterion for a good $\ell=2$ prediction was a match to known pure $\ell=2$ distributions obtained in the present work and in simultaneously performed measurements of the $\ell=2$ transitions leading to the 0.842 MeV and 5.49 MeV levels in $\ell=2$ distributions of the $\ell=3$ correspondence to the pure $\ell=2$ transitions leading to the 0.842 MeV and 5.49 MeV levels in $\ell=3$ correspondence to the parameters.

We have investigated the efficacy of deuteron potentials proposed by Hinterberger, et al., 51 Perey and Perey, 53 Newman, et al., 52 Schwandt and Haeberli, 54 Mermaz, et al., 55 and Cowley, et al. 98 in both the local, zero-range (LZR) and the finite-range, non-local (FRNL) versions of the DWBA. The non-locality parameters used for the proton and deuteron channels were, respectively, the standard 49 values 0.85 and 0.54. The geometry of the neutron bound-state wave function had the standard Woods-Saxon form, r_0 =1.24 fm, a=0.65 fm, and a Thomas spin-orbit term with λ =25. The depth of the bound-state potential well was always adjusted to match the experimental neutron separation energies corresponding to the various excited states of 38 K. The finite-range parameter was 0.621. 49

All calculations were carried out with no lower cut-off in the radial integration.

In addition, we investigated the "adiabatic" prescription for deuteron-proton transfer reactions, as proposed by Johnson and Soper 43 and shown to yield good results for reactions on lead, 45 f-p shell, 44 and oxygen, $^{46-48}$ targets, and a "density-dependent" damping of the $\rm V_{pn}$ interaction as proposed by Preedom. 48

When any of the conventional \$1-55,98 deuteron optical-model potentials was used, the calculated shapes of \$\ell=0\$ and \$\ell=2\$ distributions were in much better agreement with our experimental test cases in the FRNL approximation than in the LZR approximation. The best results obtained with any of the various potentials \$51-55\$ appear to be obtained with the "Set I" parameters of Hinterberger, et al. \$51\$ (see Table 12), which is gratifying, since this potential set is probably the best grounded in terms of mass and energy dependence. The Hinterberger, et al. "Set II" and the Newman, et al. potentials yielded results not too different from those of "Set I".

The critical success of the Hinterberger "Set I" parameters, relative to potentials of different origins, lies in its correct reproduction of the forward angle $(\theta_{\rm cm}^{\rm < 20^{\circ}})$ l=0 and l=2 shapes. Its principle failing, shared by all the others to a greater or lesser extent, is its overestimation of crosssections at larger angles $(\theta_{\rm cm}^{\rm > 30^{\circ}})$, a failing which grows more pronounced as the Q-values become more negative (excitation

Optical-model parameters used in the analysis of the $^{39}\text{K}(\text{p,d})^{38}\text{K}$ data. Table 12.

Particle	V _R (MeV)	r _R (fm)	a _R (fm)	$r_{ m R}$ $a_{ m R}$ $W_{ m V}$ $r_{ m V}$ $a_{ m V}$ $W_{ m S}$ $r_{ m S}$ f $a_{ m S}$ f $V_{ m SO}$ $r_{ m SO}$ $a_{ m SO}$ $r_{ m C}$ $(f_{ m m})$	r _V (fm)	a _V (fm)	Wsf (MeV)	rsf (fm)	a _{sf} (fm)	V SO (MeV)	rso (fm)	a so (fm)	r _o (fm)
Proton ^a	45.66	1.17	0.75	1.17 0.75 5.0 1.32 0.53 3.36 1.32 0.53 6.2 1.01 0.75 1.17	1.32	0.53	3.36	1.32	0.53	6.2	1.01	0.75	1.17
Deuteron (FRNL and DFRNL)	87.48-0.35 E _{cm}	1.25	1.25 0.729				13.0	1.25	0.766	0.9	1.25	13.0 1.25 0.766 6.0 1.25 0.729 1.3	e.
Deuteron ^C (ADIABATIC)	103.79 ^d	1.17	0.779	1.17 0.779 1.08 ^d 1.29 0.589 17.53 ^d 1.29 0.583 6.2 1.01 0.75 1.17	1.29	0.589	17.53	1.29	0.583	6.2	1.01	0.75	71.1
Neutron Bound State	Adjusted to match separation 1.24 0.65 energy	1.24	0.65							λ=25			1.24

a Reference 37.

DRef. 51 averaged parameter Set 1 of Hinterberger, et al.

^CRef. 43 neutron and proton parameters from Ref. 37.

 $^{\rm d}_{\rm Values}$ shown are for E_x=0.000 MeV onlj; Q-dependence as given in Ref. ³⁷.

energies get higher, binding energies of transferred neutrons become larger). Experience led us to expect that both the "abiabatic" 43 and the "density-dependent" 48 alterations to the conventional DWBA procedure would improve the predictions at these larger angles. The "adiabatic" potential, designed to account for effects resulting from disassociation of the deuteron, is not related to actual deuteron elastic scattering data but is constructed from proton and neutron optical-model potentials (taken from Ref. 37 in the present instance) according to a particular prescription. 43,47 The adiabatic-potential calculations were carried out in the LZR approximation, since the FRNL corrections did not yield significantly different results.

The "density-dependent damping" of the V_{pn} interaction, ⁴⁸ motivated by a paper by Green, ⁶⁹ provides an alternate means to reduce DWBA cross-sections at larger angles. We have chosen the damping factor $F(r)=(1.0-1.845_{\rho}(r)^{2/3})$, where $\rho(r)=0.17[1+\exp(x)]^{-1}$, $x(r-r_0A^{1/3})/a$ and " r_0 " and "a" are the radius and diffusivity of the neutron bound-state well. The density-dependent V_{pn} damping was studied in conjunction with FRNL calculations which used the Hinterberger, et al. "Set I" deuteron potential.

We have analyzed our data in detail with the following DWBA calculations (see Table 12): (1) The Becchetti-Greenlees 37 proton parameters and Hinterberger, et al. 51 "Set I" deuteron parameters, using the FRNL approximation. These calculations,

henceforth referred to as FRNL, are thus completely orthodox and unadjusted. (2) This same combination of proton and deuteron parameters and computational approximations, but with the addition of the density-dependent damping of the Vpn interaction, henceforth referred to as DFRNL, and (3) The Becchetti-Greenlees proton parameters and the adiabatic deuteron parameters in the LZR approximation, henceforth referred to as ADIABATIC.

The results of these three types of DWBA calculations are compared with each other and with some of our experimental data in Figs. 19 and 20. The general characteristics of these calculations, relative to the experimentally observed $\ell=2$ and $\ell=0$ transfer distributions, are as follows. The FRNL calculations fit the pure $\ell=2$, j=3/2 observed shapes from 3° out to 50° quite well; the indications are that from 50° on out, the theoretical differential cross sections are too large. For $\ell=0$ transitions, the observed shapes are reasonably well reproduced out over the second maximum, but from there on, the theoretical predictions are much too large. In addition, the structure of the theoretical distributions begins to be flattened out for states at higher excitation energies, while the observed shapes seem almost independent of the Q-value involved.

The DFRNL calculations fit the $\ell=2$ observed shapes essentially perfectly throughout the experimental angular range covered. The agreement with the observed $\ell=0$ shapes is considerably improved over the FRNL predictions, but cross-sections are still

Figure 19. A comparison of fits to representative angular distributions from the ³⁹K(p,d) ³⁸K reaction at 35 MeV with the three chosen types of DWBA calculations. All fits were performed over the 30 to 350 angular region. The curves are identified as follows: ——DFRNL, ----FRNL, and ——ABIABATIC.

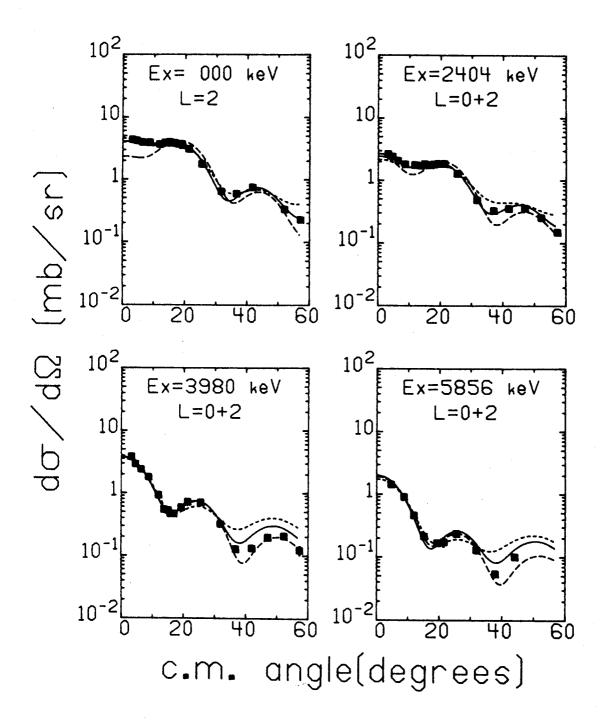


Figure 19

Figure 20. A comparison of ADIABATIC, FRNL, and DFRNL calculations (see text and Table 12) with $\ell=0$ transitions in the $^{34}S(p,d)^{33}S$ reaction at 35 MeV.

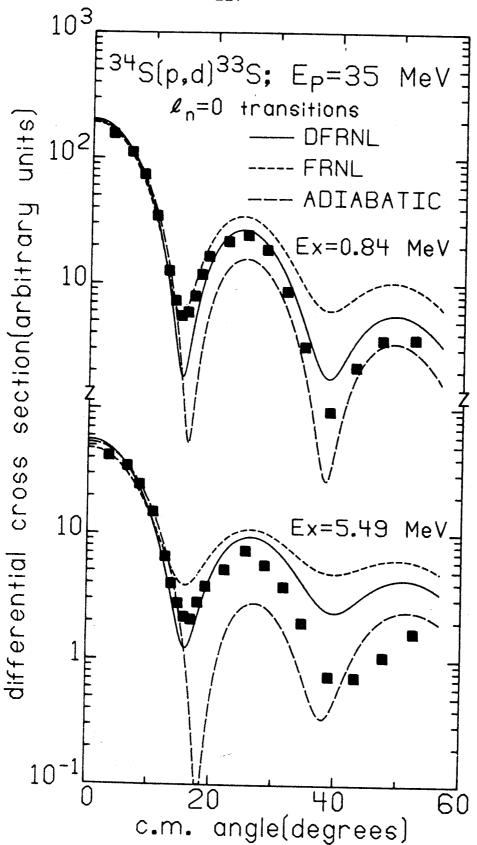


Figure 20

somewhat too large beyond 30°, and the undesired trend of shape with Q-value persists.

Finally, the ADIABATIC calculations do not match the forward angle ($\theta_{\rm cm}^{<}15^{\rm O}$) behavior observed for the $\ell=2$ distributions, although for $\theta_{\rm cm}^{>}15^{\rm O}$, the fits to the data are as good as the FRNL results (but still not as good as the DFRNL results). The differential cross sections predicted for $\theta_{\rm cm}^{>}20^{\rm O}$ for the $\ell=0$ distributions are indeed lower than those obtained with the FRNL and DFRNL calculations, but over the $3^{\rm O}-40^{\rm O}$ region, the agreement with experiment is worse for states at high excitation energy and only comparable for lower excited levels.

IV.4.B. Analysis of Experimental Angular Distributions

Our measurements of the angular distributions of the intensities with which states in 38 K are populated in the 39 K(p,d) 38 K reaction at 2 E = 35 MeV are presented in Figs. 21-24. Some states included in the table of excitation energies are not shown because they were not observed at a sufficient number of angles. The solid curves through the data points are fits of the DFRNL calculations described above. These fits, and the resulting spectroscopic factors, were obtained by minimizing the quantity

$$\chi^{2} = \frac{1}{N} \sum_{i=1}^{N} \left[\left(A_{ij} \frac{\frac{d\sigma}{d\Omega}(\theta_{i})_{ij,DWBA}}{2j+1} - \frac{d\sigma}{d\Omega}(\theta_{i})_{exp} \right) / \Delta\sigma_{i} \right]^{2}$$

through the adjustment of the coefficients $A_{\ell j}$. Here, $\frac{d\sigma}{d\Omega}(\theta_i)_{\ell j, DWBA}$ are the numbers output from the DWUCK program for angles θ_i , $\frac{d\sigma}{d\Omega}(\theta_i)_{exp}$ are the experimental differential cross-sections and $\Delta\sigma_i$ are the statistical plus estimated relative systematic errors in the experimental numbers. Values of $\ell=0$ plus 2, or 1 plus 3, were used except in special cases where known spin assignments precluded mixing. The number of data points, N, included all observations in the angular range $3^{\circ}-35^{\circ}$. The spectroscopic factors, weighted by the isospin Clebsch-Gordon factors, are then obtained from the relation

$$A_{\ell j} = 2.29 C^2 s_{\ell j}.$$

In Table 13 we list the excitation energies, \(\ell \text{-value assign-ments} \) and spectroscopic factors for all the states whose angular distributions we considered analyzable. The DFRNL DWBA calculations were used in extracting these numbers.

We carried out the same fitting procedure, again with the DFRNL predictions, including all data points out to 60°. The maximum changes in the resulting spectroscopic factors were 10%. We also carried out the fitting procedure for all distributions, in the 3°-35° angular range, with the FRNL and ADIABATIC DWBA predictions. The DFRNL results are compared to the FRNL and ADIABATIC results and to results of previous experiments and analyses in Table 14. Only those states previously observed are included in this table, to keep the size

Figure 21. Experimental angular distributions for states in ³⁸K, as observed in the ³⁹K(p,d) ³⁸K reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the amount of the l=0 component in mixed l=0-l=2 distributions.

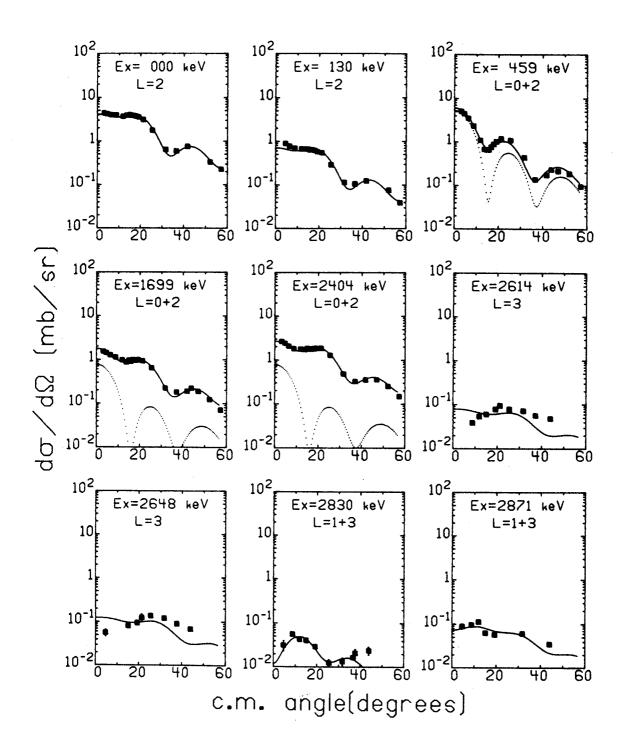


Figure 21

Figure 22. Experimental angular distributions for states in ³⁸K, as observed in the ³⁹K(p,d) ³⁸K reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 35°. The dotted curves show the amount of the \$\ell=0\$ component in mixed \$\ell=0-\ell=2\$ distributions.

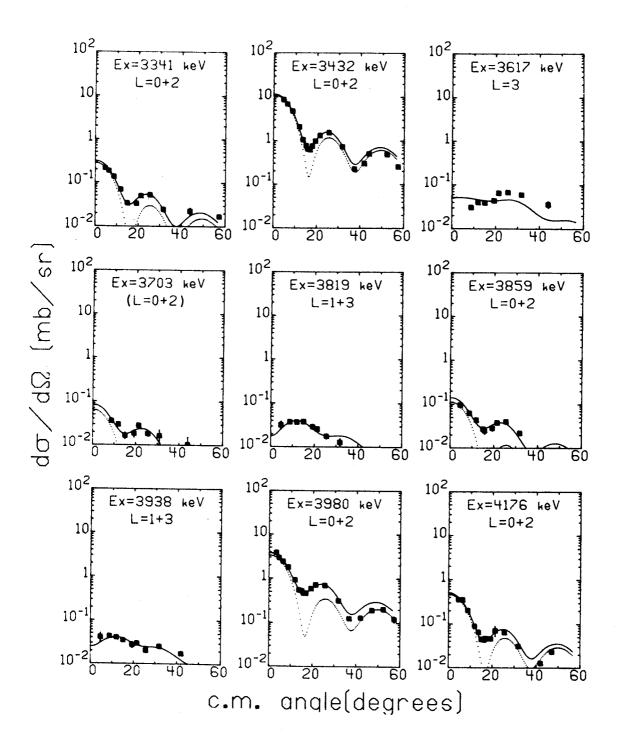


Figure 22

Figure 23. Experimental angular distributions for states in ³⁸K, as observed in the ³⁹K(p,d) ³⁸K reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 350. The dotted curves show the amount of the l=0 component in mixed l=0-l=2 distributions.

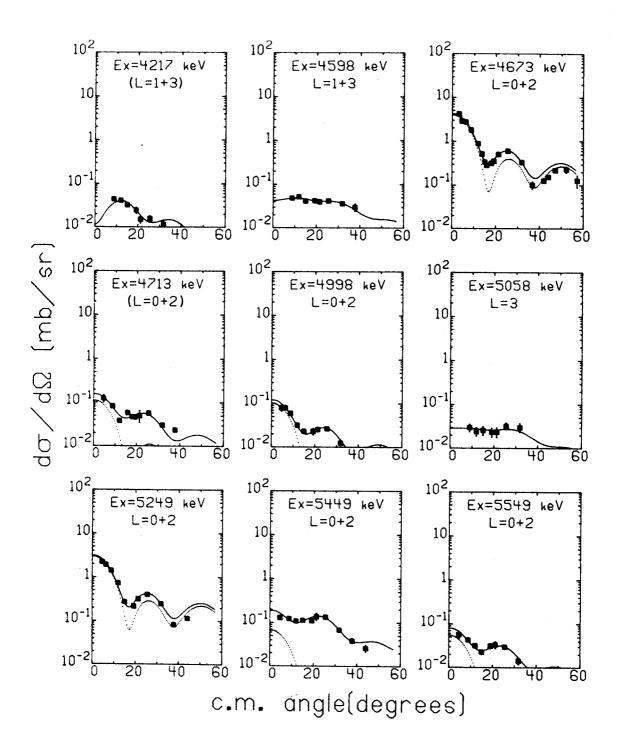


Figure 23

Figure 24. Experimental angular distributions for states in ³⁸K, as observed in the ³⁹K(p,d) ³⁸K reaction at 35 MeV. The solid curves are fits of the DFRNL calculations to the data in the angular range from 30 to 35°. The dotted curves show the amount of the \$\mathscr{l}=0\$ component in mixed \$\mathscr{l}=0-\mathscr{l}=2\$ distributions.

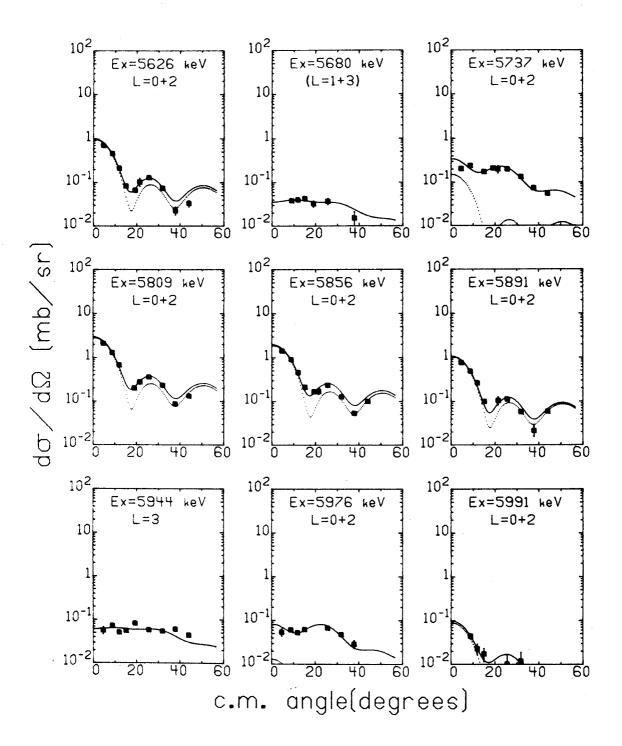


Figure 24

Table 13. Experimental values of ℓ and C^2S_ℓ , obtained from the DFRNL analysis for transitions from ^{39}K to ^{38}K as observed in the present investigation. All values are normalized so that C^2S_ℓ for the ground state is 1.75. The assumed j-values are 3/2 for ℓ =2, 3/2 (n=2) for ℓ =1, and 7/2 for ℓ =3.

E _x (keV)	J ^π ,Τ ^а	L	c ² s _l	E _x (keV)	J ^π ,T ^a	L	c²s _ℓ
000	3 ⁺ ,0	2	1.75	4217		(1,3)	0.02 ,0.01
130	0,1	2	0.31	4598		1,3	0.005,0.04
459	1,0	0,2	0.13 ,0.32	4673	(1,2)+,1	0,2	0.19 ,0.25
1699	1,0	0,2	0.02 ,0.57	4713		(0,2)	0.005,0.05
2404	2 ⁺ ,1	0,2	0.03 ,1.26	4998		0,2	0.005,0.02
2614		3	0.05	5058		3	0.03
2648	(2,3)	3	0.08	5249	(1,2)+,1	0,2	0.16 ,0.17
2830	(0,3)	1,3	0.02 ,0.01	5449		0,2	0.004,0.15
2871	(0,3)	1,3	0.01 ,0.05	5549		0,2	0.003,0.03
3341	ı ⁺ ,0	0,2	0.01 ,0.02	5626		0,2	0.06 ,0.05
3432	2 ⁺ ,0	0,2	0.43 ,0.43	5680		(1,3)	0.003,0.04
3617	•	3	0.04	5737		0,2	0.009,0.26
3703		(0,2)	0.003,0.02	5809	(1,2)+	0,2	0.17 ,0.16
3819		1,3	0.01 ,0.02	5856	(1,2)+	0,2	0.11 ,0.12
3859		0,2	0.005,0.03	5891	(1,2)+	0,2	0.06 ,0.04
3938		1,3	0.01 ,0.02	5944		3	0.08
3980	(2) ⁺ ,1	0,2	0.14 ,0.42	5976		0,2	0.001,0.10
4176	• •	0,2	0.02 ,0.03	5991		0,2	0.006,0.01

^aReferences 84, 85, 87, 92, 93, 94.

manageable, but these suffice to indicate the trends and scatter of the spectroscopic factors as functions of the details of the DWBA calculations.

IV.4.C. Assignment of &-values

Of the forty-six ³⁸K levels observed in the present investigation, thirty-six can be assigned at least tentative values for the orbital angular momentum quantum numbers of the neutrons transferred in the process of their formation (see Table 13). Twenty-four levels are assigned pure \$\ell=2\$ or a combination of \$\ell=0\$ and \$\ell=2\$ transfers. The basis for these assignments is typically an excellent and unambiguous fit to the the experimental distribution with a mixture of calculated \$\ell=0\$ and \$\ell=2\$ shapes. Most of the transitions having significant \$\ell=0\$ strength are also easily recognized simply on the basis of the differential cross-sections for this type of transfer, which is clearly evident in the 3°-13° portion of our angular distributions.

Assignments of negative-parity ℓ -values (ℓ =1 and 3) could not, in general, be made with the assurance possible for the positive parity cases. This was because the experimental distributions were rather featureless (except for a few examples dominated by ℓ =1) and because the calculated ℓ =3 shape does not appear to fit the data as well as those for ℓ =0, 1 and 2. Consequently, it is possible in many cases to get as reasonable

a fit to the data with $\ell=2+4$ shapes as it is with $\ell=1+3$ shapes. In addition, there is the uncertainty as to whether some of the weakest, flattest distributions observed are even characteristic of a single-step direct transfer. We have assigned a negative parity ($\ell=3$ and/or 1) to twelve of the levels observed. Many of these assignments, however, are dependent upon an assumption which rules out the possibility of significant $\ell=4$ transfer strength in the present experiment.

Questions involving the agreement of the present assignments with previous results, their relationship to theoretical
studies, and the degree of certainty with which the presence
or absence of a particular 1-value component can be detected
in a given transition will be discussed in the following sections.

IV.4.D. <u>Discussion of Values Extracted for C²S</u>

In the present study, we are not concerned with extracting the absolute magnitude of the single nucleon transfer spectroscopic factors. We are interested primarily in trying to get some measure of the reliability of relative spectroscopic factors for a particular &-transfer as a function of Q-value (or the separation energy for the picked-up neutron), and of the relative values for different (&=2 vs. &=0) &-transfers. The latter point reduces, in the limit, to the question of the certainty with which a weak component of one mode of &-transfer can be identified in a transition dominated by the other. This,

of course, is important beyond just the spectroscopic factor, since the presence of a particular ℓ often has direct implications for the spin of the residual state.

The accuracy with which the Q-dependent effects on overall cross-section magnitudes are reproduced by DWBA calculations is difficult to pin down, but serious difficulties have been noted. 79,94 We mentioned in a previous section that details of the angular distributions as a function of Q-value are not well handled in all cases. We have merely tried rather different sets of optical-model parameters and examined the consistency of the results. This was also the tack used to examine the accuracy (really only the consistency) of the relative magnitudes of the peak cross-sections for different £ transfers. The results of these studies, covering not only the three types of DWBA calculations already discussed here in some detail, but also a good many others, indicate that most reasonable DWBA formulations for the (p,d) reaction yield consistent results within the domain of the residual nuclear states studied here. The extent to which these results are "correct" can be further explored by comparing extracted spectroscopic factors with those obtained from other reactions, as will be done in a following section.

The spectroscopic factors extracted from a fit to (generally) mixed- ℓ angular distributions contain Q-dependent and ℓ -dependent uncertainties arising from errors and lack of completeness in the data set, and from failures of the

Table 14. Experimental values of C^2S_g for the transitions from 39 K to 38 K. The absolute values for the ground state are presented in parentheses. All other values are normalized such that $C^2S=1.75$ for the ground state.

130 0*,1 · 2 159 1*,0 0 1699 1*,0 0 2404 2*,1 0	1.75 (3.52)	1.75						
0,1. 1,0 1,0 1,0	0.31	(2,51)	1.75	1.75 (1.83)	1.75	1.75	0	ų,
1,0 1,0 2,1		0.31	0.31	0.25	0.328	54.0	0.25	0.26
1 ⁺ ,0	0.13	0.16	0.12 0.33	0.10	0.19	0.18		
2+,1	0.02	0.02	0.04	0.00	0.05 0.56	<0.07 0.68		
	0.03	0.00	0.05	0.08	0.27	<0.14	1.25	1.25
2648 ,0 1 3	0.05	0.07	90.0	60.0	0.02	0.13		
3432 2*,0 0	0.43	0.14	0.35	0.32	0.51	0.51 0.22		
3980 (1,2) ⁺ ,1 0	0.14	0.16	0.13	90°0 0°48	0.23 0.31	0.23 0.34	0.13	0.08
4673 (1,2) ⁺ ,1 0	0.19	0.20	0.15	464.0	0.21 0.15	0.29	0.31	0.24
5249 (1,2) ⁺ ,1 0	0.16	0.16	0.13		0.18	0.23	0.16	0.12
5449 (1,2) ⁺ ,0 0	0.00	0.00	0.01		0.02			
5809 (1,2) ⁺ 0	0.17	0.16	0.13 0.24					
\$856 (1,2) [†] 0	0.11	0.11	0.09				0.39	0.32
5891 (1,2) ⁺ 0	90.0	0.06	0.05					
^a Present work; all £=2 spectroscopic factors for d ₃ / ₂ transfer. ^b Reference 85. ^c Preserance 85. ^c Preserance 86.	ectroscopic	factors	for	Reference 94. fReference 79. $gc^2s_0,1/z^20.03$	Reference 94.	eported.		

Creference 86; radial cut-off=2.8 fm. dreference 64; $\rm E_{3}^{-1}$ =10 MeV; $\rm C^2S_2,_{3/2}$ below 2.5 MeV, $\rm C^2S_2,_{5/2}$ above 2.5 MeV. DReference 85.

DWBA curves to exactly reproduce the shapes of pure -1 distributions, as well as from the more fundamental uncertainties By measuring the in cross-section trends mentioned above. experimental distributions in to 3° we have insured that the $\ell=0$ spectroscopic factors are free from the extra uncertainties chronic in many previous studies, in which the data extends in to cover only the second maximum of the $\ell=0$ shape. intrinsic cross-section of the DWBA-calculated &=0 transition at 3° is ~20 times the magnitude of the l=2 prediction at its Hence, our extracted values for C²S(l=0) are extremely secure in an experimental sense. That is, there is no way to reproduce the shape of an experimental distribution which has a significant peaking at 0° without putting in essentially the total amount of \$\ell=0\$ strength obtained in our The exact amount of \$\ell=0\$ admixture in a predominantly £=2 distribution can be given to an accuracy sufficient for any meaningful comparison with theoretical predictions. more interesting question, involving weak to non-existent $\ell=0$ components, concerns the limit to which their presence can definitely be assigned. The better the quality of the data and the better the theoretical fit to pure &=2 shapes, the more stringent a criterion may be employed. We think that in the present work the presence of an &=0 component is unambiguously established if $C^2S(\ell=0) \ge 0.005$.

The problem of extracting accurate $\ell=2$ spectroscopic factors from shapes displaying significant $\ell=0$ character is

much more difficult than the converse problem. Since the intrinsic magnitudes of the $\ell=2$ DWBA cross-sections are so much smaller than those of the $\ell=0$ predictions, and are also relatively unstructured, the amount (and the uncertainty thereof) of observed $\ell=2$ strength in an apparently $\ell=0$ experimental shape can be quite significant in terms of nuclear structure predictions. Unless one has perfect $\ell=0$ DWBA predictions and essentially perfect data, this problem seems impossible to overcome. An objective, integrating-fit criterion such as we have used is probably not the best approach to extracting $\ell=2$ components unless the theoretical $\ell=0$ fits are quite good. It is quite possible that the $\ell=2$ strength assigned by the fit serves predominantly to compenstate for the principle defect in the l=0 predicted shapes. We think that the fits of the DFRNL predictions to the data are good enough to justify an automatic, non-subjective analysis procedure. Some of the lack of consistency which crops up in the comparison between spectroscopic factors extracted with the three different calculations surely arises from deficiencies in the FRNL and ADIABATIC &=0 shapes.

IV.5. Discussion of Results

IV.5.A. Comparison with Previous Experimental Results

All levels in 38 Ar (T=T $_z$ =1) should have analogues in the 38 K spectrum which have essentially the same properties.

Experiments 79,94 with the 39 K(d, 3 He) 38 Ar reaction show that the 0⁺ ground state and the 2⁺ first excited state at 2.167 MeV are strongly populated with l=2 transfer and that 2⁺, 2⁺, 2⁺, and (1,2) + levels at 3.937, 4.565, 5.157, and 5.552 MeV, respectively, 95 are strongly populated via $\ell=0$ transfer. It was explained in Ref. 94, before unique spins for the higher states were known, that the spectroscopic factors for states below 6 MeV excitation observed in the 39 K(d, 3 He) 38 Ar reaction could be understood in terms of a $(d_{3/2}^{-1})_{J=3/2}$ model for ^{39}K , $(d_{3/2}^{-2})_{J=0}$ and 2 wave functions for the ground and first excited states (d_{3/2} pickup) and $(d_{3/2}^{-1}s_{1/2}^{-1})_{J=1,2}$ wave-functions for the higher lying %=0 strength. Since only one 1 and one 2 state can be formed from the $s_{1/2}$ - $d_{3/2}$ coupling and four $\ell=0$ states are observed, it is obvious that fragmentation of the \$\ell=0\$ strength into states arising from other configurations occurs. It was argued in Ref. 94 that the fragmentation most probably involved 2⁺ states (since confirmed), and that the extra two 2⁺ states had their origins in f-p shell configurations rather than in $d_{5/2}$ hole excitations. The state at 5.55 MeV was suggested to have $J^{\pi}=1^+$.

All of these strongly excited levels in 38 Ar should be observed, with similar relative strength, in the 39 K(p,d) 38 K spectra. The total number of 38 Ar states presently known to exist below 6 MeV excitation is 21. Our present high resolution data may allow the observation of others. The analogues of the first five strongly excited 38 Ar levels are observed at 130, 2404, 3980, 4673, and 5249 keV. Relative to the lowest 0 , T=1 state, the energy shifts of these five

excited states in 38 K, relative to 38 Ar, are +107, -87, -22, and -42 keV, respectively.

The analogue of the 5.552 ("5.85") MeV level in 38 Ar observed in (d, 3 He) is not clearly identifiable in 38 K. We observe three ℓ =0 transitions in the 5800-5900 keV region in the present experiment which would not have been resolved in the (d, 3 He) study. However, only one (at 5.552 MeV) positive-parity level is known to exist 95 in the appropriate energy region of 38 Ar, implying that the ℓ =0 transition observed in (d, 3 He) proceeds to a single state. All this implies that two of the three ℓ =0 states we observe in 38 K near 5.85 MeV excitation have T=0. However, the ℓ =0 spectroscopic strength observed in (d, 3 He) is significantly greater than that of any one of the 5.85 MeV states in 38 K.

The consistency between the spectroscopic factors extracted from the (d, ³He) data and the (p,d) data can be inspected in Table 14. The apparent analogues of the first five strongly excited levels in ³⁸Ar have ³⁹K(p,d) ³⁸K spectroscopic factors consistent with the (d, ³He) values, the largest deviation occuring for the 4.673 MeV state. Thus, it seems likely that the failure to find a single state in the 5.85 MeV region of ³⁸K which has spectroscopic strength comparable to the (1)⁺,T=1 state at the corresponding energy in ³⁸Ar, together with the other features of the situation just discussed, is evidence of almost complete mixing of the 1⁺,T=1

state which must occur in this region in ³⁸K with one, and probably two, close lying T=0 neighbors. Indeed, the summed spectroscopic strength of the three ³⁸K levels at 5.85 nicely equals the strength of the (presumed) single state in ³⁸Ar.

It is not possible to establish further isospin assignments in 38 K via correspondence between the 38 K and 38 Ar level schemes because the level densities are high relative to the average Coulomb shifts and because proton pick-up data comparable to the present neutron pick-up work does not exist.

The agreement between the present results and those of previous neutron pick-up studies of 38 K seems quite good, considering the limitations of the older data. It is perhaps interesting that, on the average, all of the neutron pick-up results exhibit the same deviations from the proton pick-up results, namely a larger C^2 S(ℓ =2) for the first ℓ 0, T=1 state and a smaller ℓ 2 S(ℓ =0) for the 4.67 MeV, ℓ 2 state.

IV.5.B. Comparison of Results with Structure Theory

Pick-up spectroscopic factors predicted for $^{39}\text{K}_{\div}^{38}\text{K}$ transitions are compared with the present experimental results in Table 15. The listed theoretical numbers are averages of the predictions derived from the two most successful Hamiltonians presented in Ref. 3, Kuo-type Hamiltonians $^{12.5\text{p}+}^{17}\text{O}$ and $^{11.0\text{h}+\text{ASPE}}$. The agreement appears quite

Table 15. Experimental and theoretical values of C²S for single neutron pick-up from ³⁹K.

Ex (keV) ^a	J ^π ,Τ	L	DFRNLa	THEORY
000	3 ⁺ ,0	2	,1.75	,1.72
130	0+,1	2	,0.31	,0.23
459	1+,0	0,2	0.13,0.32	0.13,0.40
1699	1+,0	0,2	0.02,0.57	0.04,0.46
2404	2+,1	0,2	0.03,1.26	0.01,1.20
3432	2 ⁺ ,0	0,2	0.43,0.43	0.43,0.15
3980	(1,2)+,1	0,2	0.14,0.42	
4673	(1,2)+,1	0,2	0.19,0.25	0.58,0.05
5249	(1,2)+,1	0,2	0.16,0.17	
5809	(1,2)+	0,2	0.17,0.16	·
5856	(1,2)+	0,2	0.11,0.12	0.37,0.00
5891	(1,2)+	0,2	0.06,0.04	

^aPresent Work.

b_{Reference 3.}

impressive, and seems to confirm the essential validity of this particular approach to calculating low-lying positive parity states at the top of the s-d shell. While the comparison definitely confirms the success of the Kuo matrix elements relative to the other interactions studied, the differences between the individual predictions of these two interactions were too small to be resolved. Indeed, it would seem to be almost beyond the scope of single nucleon pick-up experiments to meaningfully discriminate between the two sets of wave-functions.

The density of states observed in 38 K is far in excess of what is predicted by the $d_{5/2}$ - $s_{1/2}$ - $d_{3/2}$ shell-model calculations just discussed, which so successfully predict the observed apportionment of $\ell=0$ and $\ell=2$ (mostly but not all, $d_{3/2}$) strength among the low-lying levels. The drastic fragmentation of the $\ell=0$ spectroscopic strengths to "extra" T=1 levels provides another view of the existence and significance of states which should arise from f-p shell configurations. All s-d shell calculations firmly exclude any reasonable supposition that the extra T=1 states below 6 MeV excitation, which cannot be contracted from $d_{3/2}$ - $s_{1/2}$ couplings, arise from $d_{5/2}$ excitations. The $(d, ^3$ He) data support this view, indicating that the next $\ell=2$ level above the 2^+ first excited state falls at 7 MeV excitation.

IV.6. Conclusions

We have found that the angular distributions of the (p,d) reaction on ³⁹K, using a proton energy of 35 MeV and covering 6 MeV of excitation in the residual nucleus, can be successfully analyzed with DWBA calculations which employ the most broadly based proton and deuteron optical-model potentials available. The finite-range, non-local DWBA calculations which use these parameters fit both $\ell=0$ and $\ell=2$ distributions quite well in the 30-250 range. At larger angles, the predicted cross-sections do not drop off as rapidly as do the data. Use of a deuteron potential constructed by folding neutron and proton potentials, or use of a damped V_{DN} interaction serve to improve agreement at larger angles. The density-dependent damping procedure yields the best fits to the present data. Any of these DWBA prescriptions yields stable and theoretically sensible spectroscopic factors if only the 30-200 data are used.

Many new levels have been observed in the present experiment and assigned excitation energies accurate to 1-3 keV. The detailed angular distribution measurements permitted the assignment of a positive parity and spin limits to many of the observed levels, and tentative negative parity to many others. The spectroscopic factors extracted for the more strongly populated states are, in general, consistent with results of previous neutron and proton pick-up experiments. The

results for the low-lying positive parity levels provide conclusive verification for the relevant predictions of recent shell-model calculations.

The details of structure observed above 3 MeV excitation are evidence of extensive effects of f-p shell configuration states, but aside from energy level schemes, no predictions from extended (s-d-f-p) shell-model calculations are yet available to compare to our results. We observe what appears to be very strong mixing between T=0 and T=1,J=1⁺ states at 5.85 MeV excitation.

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APPENDIX A

MONSTER2

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MONSTER2

MONSTER2 is the computer code used to analyze all of the nuclear emulsion plate and position-sensitive proportional counter data taken for this thesis using the MSU split-pole magnetic spectrograph. The code accepts input in the form of experimental parameters (beam energy, scattering angle, spectrograph magnetic field strength (in terms of the fieldsampling NMR frequency) and focal-plane-position settings), reactions appropriate to the experiment and spectral peak specifications (excitation energy, or centroid and total counts). Relativisitic reaction kinematics are calculated with a modified version of the function KINE. 96 MONSTER2 is multi-functional with options to perform the following (1) transform cross-sections from laboratory to coordinates, (2) perform spectrograph center-of-mass (CM) calibration and evaluate excitation energies, (3) predict positions of particle groups in the spectrograph focal plane, (4) identify contaminant peaks and (5) perform multi-angle excitation energy averaging and cross-section compilation.

1. CROSS-SECTION TRANSFORMATION: When particle group yields are input, they are multiplied by a user-supplied normalization factor to yield an absolute cross-section in the laboratory. They are converted to a CM cross-section by multiplying by $\sigma_{\rm CM}/\sigma_{\rm LAB}$ as calculated in KINE

for the particular reaction and Q-value under consideration. The statistical error in the CM cross-section is automatically calculated.

2. EXCITATION ENERGIES: Nuclear reactions are typically designated as A(a,b)B, where A is the target nucleus, a the projectile, b the outgoing particle, and B is the residual nucleus. B may be left in any of its states for which the transition is energetically and quantum mechanically allowed. Accurate observation of the momentum of particle b, (p), allows a precise excitation energy assignment to the appropriate level in B via reaction kinematics.

In an Enge-type split-pole spectrograph, the radius of curvature (ρ) of the outgoing particle is roughly proportional to the position in the focal plane at which it is detected. Since $p\alpha\rho$, a ρ vs. position calibration allows the determination of the particle momentum and, hence the excitation energy of the corresponding level in the residual nucleus.

The MSU spectrograph focal plane is assumed to be described by the relation 67

$$B\rho = B\rho_{KINE} + \Delta B\rho = B(\rho_{o} + \alpha D + \beta D^{2} + \alpha \delta) \qquad A.1$$

with the following definitions:

B - spectrograph magnetic field (kilo-gauss), determined from NMR frequency.

Bp - "real" particle rigidity (p=qBp, where q is the charge of the outgoing particle).

Bo KINE - particle rigidity calculated from relativistic kinematics based on the reaction, Q-value and nominal beam energy and scattering angle.

absolute focal plane peak position relative to a designated reference position, D_o, usually
 9-13 inches from the high energy end.

 ρ_{O} - radius of curvature corresponding to D_{O} .

 α , β - linear and quadratic coefficients of the expansion about D_O (\sim -0.4 and \lesssim 10⁻⁴/inch, respectively).

- a first-order estimation of the gap between abutting plates when a single spectrum is recorded on two consecutive plates in the focal plane; δ is non-zero only for particle groups falling on the second (low energy) plate.
- ΔB_{ρ} a correction to $B_{\rho}{}_{\rm KINE}$ necessitated by small, but real, variations in the nominal experimental parameters. To first order,

$$\Delta B_{\rho} = \frac{\Delta B_{\rho}}{\Delta E_{\text{beam}}} \Delta E_{\text{beam}} + \frac{\Delta B_{\rho}}{\Delta \Theta_{L}} \Delta \Theta_{L}$$
 A.2

where $\frac{\Delta B \rho}{\Delta E_{\text{beam}}}$ is evaluated for a 50 keV change in the beam

energy and $\frac{\Delta B_{\rho}}{\Delta \theta_{L}} = \frac{\Delta B_{\rho}}{\Delta T} \frac{\Delta T}{\Delta \theta_{L}}$ with $\frac{\Delta T}{\Delta \theta_{L}}$ calculated in KINE (T=particle kinetic energy) and $\frac{\Delta B_{\rho}}{\Delta T} = E_{TOT}/B\rho$ (E_{TOT} =T+particle rest mass).

When sufficient particle groups from known energy levels (reference peaks-RP) are present, one may perform a complete energy calibration on the given spectrum. Once these RP and their associated reactions and excitation energies are input, MONSTER2 calculates $B\rho_{KTNE}$ and the coefficients of ρ_{O} , α , β , $\alpha\delta$, ΔE_{beam} , and $\Delta\theta_{L}$ (see equations A.1 and A.2) from the nominal input beam energy and scattering angle. ρ_0 , α , β , ΔE_{beam} , $\Delta \Theta_L$, and $\alpha\delta$ (when δ is not constrained to be zero) are then calculated via a least-squares fit to the RP energies. Any of the variables may be held constant and error messages are issued if the data is insufficient, or incorrect (ΔE_{beam} >100 keV or $\Delta \Theta_L$ >20). If the fit is reasonable, i.e., no error flags, the appropriate corrections to the beam energy, scattering angle and plate gap are made and the entire spectrum is analyzed, resulting in excitation energies for all peaks and reactions. If particle group yields are also input, lab-to-CM crosssection conversion takes place automatically.

2B. If the number and/or type of known reference levels is not sufficient to perform a complete calibration for a given spectrum, the user may opt to use the approximate parameters stored in MONSTER2. 67 In this case, $^{\delta}$, $^{\Delta E}_{beam}$,

and $\Delta\theta_L$ are assumed to be zero, i.e., all kinematics are calculated using input beam energy and scattering angle values, and a plate gap is specified by the user. α and β are calculated as a function of focal plane orientation (input as the parameters DS and DL), D_O is assumed to be 10 inches, and ρ_O is calculated on the basis of the first reference peak position.

When operating in this mode, insertion of one reference level forces all other peaks to be analyzed relative to it using the available calibration parameters. If more than one RP is specified from the same or different reactions, MONSTER2 also performs a linear particle momentum match to obtain a best fit to all reference This results in an effective adjustment of α . energies. Table Al shows the extent to which this fitting procedure can compensate for errors in the nominal experimental and calibration parameters. The trial errors in Table Al, except AB, were chosen as approximate maximum uncertainties usually associated with the respective parameters. present, β appears to be the most important single parameter for spectra covering more than ~10 inches of focal plane distance. Unfortunately, it is also the most poorly known, the values for β currently stored in MONSTER2 are based on theoretical predictions and prove to be very different from those calculated in several individual calibration runs on actual spectra. The change in β considered

Table Al. Extrapolations from the MONSTER2 momentum matching fits to known energy levels. Nominal energies and calibration parameters were obtained from a complete calibration run on the test spectrum. All other energies (MeV) are obtained from a fit to the first three (0.000, 0.130, 0.459 MeV) levels after the indicated shift the given parameter had been assumed.

					
Nominal	ΔE _{beam} =+35 keV	ΔΘ _L =+0.3 ^O	Δα=-1%	$\Delta \beta = 3 \times 10^{-5}$	Δf _s =+1%
0.000	0.000	0.000	0.000	0.000	0.000
0.130	0.130	0.130	0.130	0.130	0.130
0.459	0.459	0.459	0.459	0.459	0.459
1.699	1.698	1.698	1.698	1.698	1.699
2.403	2.402	2.402	2.402	2.402	2.402
3.431	3.430	3.430	3.430	3.429	3.430
3.977	3.978	3.977	3.977	3.976	3.978
5.249	5.248	5.248	5.248	5.245	5.248
5.890	5.891	5.890	5.891	5.887	5.891
7.115	7.114	7.113	7.113	7.107	7.113
8.236	8.235	8.233	8.234	8.226	8.234
9.118	9.117	9.116	9.116	9.106	9.116

in Table Al serves to indicate the effect of uncertainties in this parameter. The fitting procedure compensates for the other uncertainties to <0.5 keV/MeV to 9 MeV above the fitting region and can handle β uncertainties reasonably well over shorter extrapolation ranges. Accuracies can be significantly improved using the option to manually adjust α and β or by the use of contaminant peaks (see 4.) as additional reference levels in "unknown" regions of the spectrum.

- 3. PARTICLE GROUP POSITIONS: A knowledge of particle group placement in the spectrograph focal plane is useful not only for experimental set-up, but also in preliminary data analysis. Peak positions for specified reactions may be predicted with MONSTER2 from the experimental parameters and appropriate excitation energies. The positions are predicted, and listed in order, using the internal calibration parameters and the inverse of the excitation analysis process. Although uncertainties in beam energy and precise scattering angle impose the main limitation on the absolute position accuracy, relative spacings of known levels from the same and different reactions have been reproduced to <0.2 mm in test case comparisons with actual plate data.
- 4. CONTAMINANT IDENTIFICATION: Reaction products from target impurities often fall on the focal plane in the same region as the specific particles under investigation. The

specification of any "reasonable" reaction requires that MONSTER2 analyze every peak as though it were produced by that reaction in the pertinent experimental configuration. Comparison of the output excitation energies with known impurity levels may allow one to identify contaminants or particle groups in the spectrum which are different from those being studied. From example, the $^{16}\text{O}(\text{p,d})^{15}\text{O}_{0.000}$, the $^{12}\text{C}(\text{p,d})^{11}\text{C}_{0.000}$, and the $^{39}\text{K}(\text{p,t})^{37}\text{K}$ peaks seen in the present studies were all identified in this manner, usually within $^{\pm}3$ keV when the fitting procedure was used with known levels from target nuclei.

assigned on the basis of 2 or more spectra. MONSTER2 can search on up to 10 spectra input on the same job and perform an average of appropriate excitation energies, weighted by the raw yield for the appropriate peaks. One can also punch corresponding differential cross-sections, yielding angular distributions for specific energy levels in given residual nuclei.

APPENDIX B

ELASTIC SCATTERING DATA

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All of the (p,d) data presented herein has been normalized by comparison with proton elastic scattering data. The (p,d) and (p,p_0) spectra for each target were recorded with a single-wire proportional counter under identical experimental conditions, except for an appropriate adjustment of the spectrograph magnetic field. Consequently, with proper relative data normalizations, a knowledge of the absolute cross-section to observed proton ratio for the (p,p_0) data allows the observed deuteron cross-sections to be expressed in an absolute manner.

Figure B1 shows the spectra recorded from proton scattering on the ²³Na-³⁵Cl, ²³Na-³⁷Cl, and ³⁹K targets at 40°. Angular distributions were recorded from 25° to 50° at 5° intervals. The distributions are shown in Figs. B2, B3, and B4 normalized to optical-model calculations using the Becchetti-Greenlees ³⁷ parameters for the appropriate masses. The Na and Cl experimental cross-sections for the two sodium-chloride targets are presented in the observed relative configuration at each angle.

Figure Bl. Proton elastic scattering spectra recorded at 40° with a single-wire proportional counter.

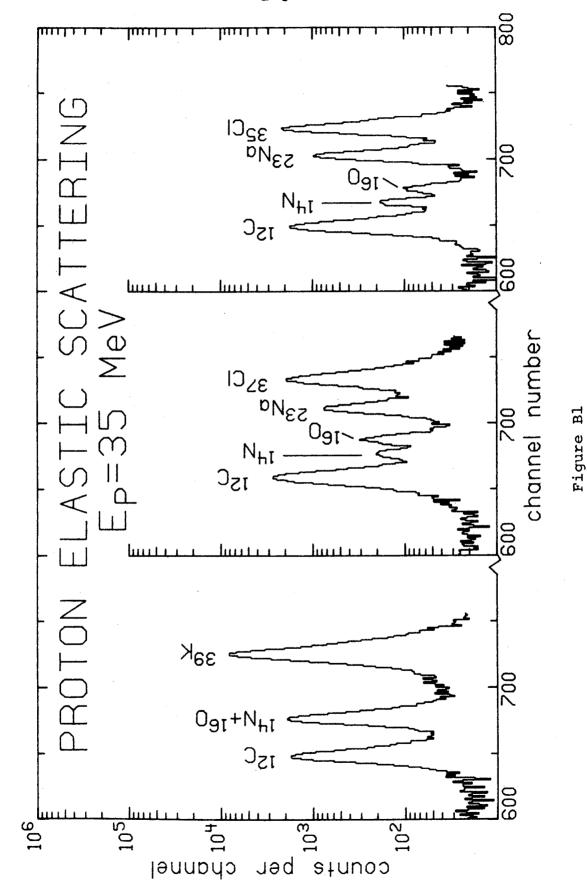


Figure B2. Measured proton elastic scattering differential cross-sections for the ²³Na-³⁵Cl target.

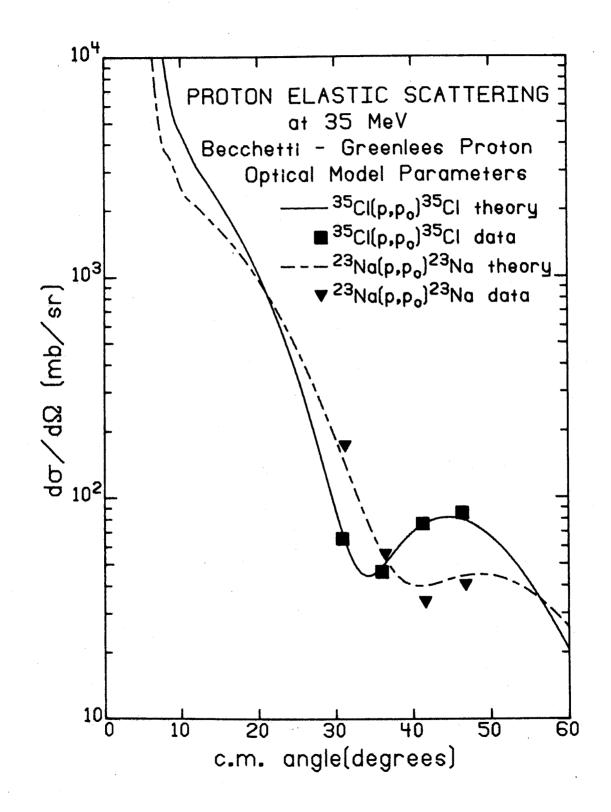


Figure B2

Figure B3. Observed proton elastic scattering cross-sections for the $^{2\,3}\mathrm{Na-^{3\,7}Cl}$ target.

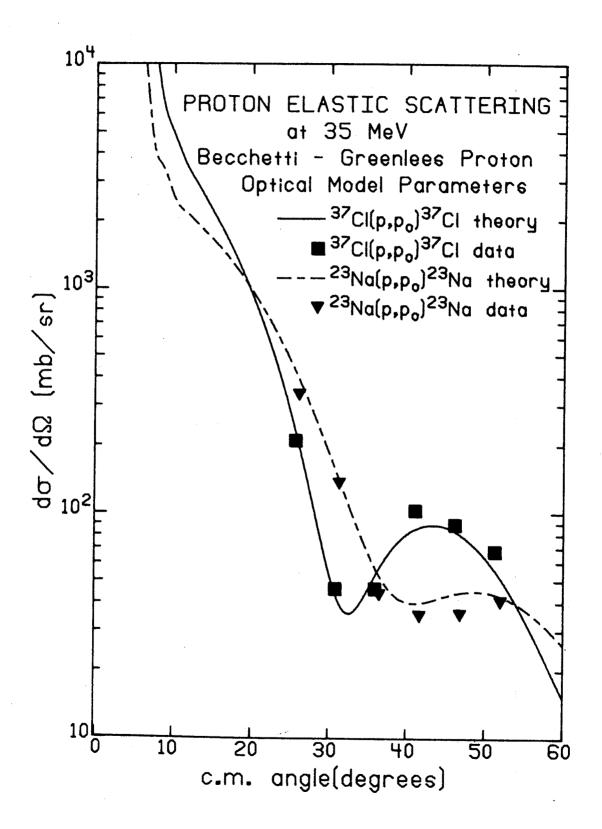


Figure B3

Figure B4. Measured proton elastic scattering cross-sections for the ³⁹K target.

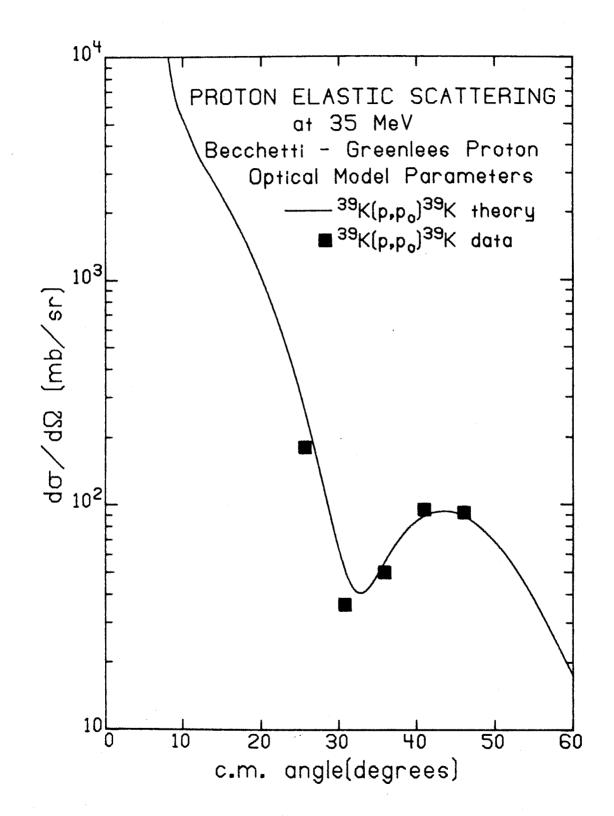


Figure B4